by Susilo Hariyanto

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## Average Based-FTS Markov Chain With Modifications to the Frequency Density Partition to Predict COVID-19 in Central Java

Susilo Hariyanto\*, Zaenurrohman, Titi Udjiani SRRM

Department of Mathematics, Faculty Science and Mathematics, Diponegoro University, Indonesia

> \*Corresponding Author Email: susilohariyanto@lecturer.undip.ac.id\*, zaenurrohman8.zr@gmail.com, udjianititi@yahoo.com

#### ABSTRACT

Every day, new Covid-19 positive cases are discovered in Central Java. Many research has used various methodologies to try to forecast new positive instances. The fuzzy time series (FTS) approach is one of them. Many FTS are now in development, including the FTS Markov Chain. The duration of the gap in the FTS must be determined carefully because it will affect the FLR, which will be used to estimate the forecast value. The average-based method can be used to determine the optimum interval length; however, other research use frequency density partitioning to determine the optimal interval length in order to produce superior predicting values. The goal of this research is to improve the accuracy of forecasting values by modifying the frequency density partition on the average based-FTS Markov Chain. The approach utilized is average-based, with the length of the interval determined by the average, the forecast value determined by the FTS Markov Chain, and the frequency density partition modified to provide the ideal interval. The average-based FTS Markov Chain approach with adjustments to the frequency density partition achieves an accuracy rate of 89.3 percent, according to the findings of this study. Because changes to the frequency density partition can produce a good level of accuracy in forecasting new positive cases of Covid-19 in Central Java, it is hoped that this modification of the frequency density partition on the average-based FTS Markov chain can be used as a model for forecasting in fields other than new positive cases. Covid-19.

Keywords: Average Based; FTS Markov Chain; Modified frequency density partitioning; COVID19; MAPE

#### INTRODUCTION

COVID-19 first appeared in the city of Wuhan, Hubei Province, China, which spread almost all over the world, including Indonesia. At the beginning of 2020, Indonesia experienced a COVID-19 pandemic, which, to this day, new positive cases are still being found[1]. The government is still thinking about how to make Indonesia free from COVID-19.

Many experts have estimated the amount of new Covid-19 positive cases in Indonesia. Forecasting is the process of predicting what will happen in the future over a lengthy period of time[2]. However, no approach for accurately forecasting anything,

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including new Covid-19 positive cases, has been developed to yet. The fuzzy time series (FTS) is one of the forecasting approaches for determining the number of new positive cases in Indonesia. The concept of fuzzy logic is used in the forecasting of FTS. Song and Chissom introduced the FTS in 1993[3], and it has since been widely developed, including the Markov method[4], Chen's method[5], Chen and Hsu's method[6], the weighted method[7], the multiple-attribute fuzzy time series method[8], the percentage change method[9], and Markov chain method[10].

Ruey Chyn Tsaur, developing fuzzy time series by merging the fuzzy time series method with the Markov chain concept [10]. Markov chain is a stochastic process in which future events only depend on today's events. Markov chain is used in the defuzzification process [11].

The determination of the length of the interval in the fuzzy time series does not have a definite formula, but the determination of the length of the interval in the fuzzy time series is based on the researcher. As a result, even if each researcher is utilizing the same data, the length of the interval will vary[3]. Even though the determination of the length of the interval is a very influential part in the formation of a fuzzy logical relationship (FLR).[12]. One method that can be used to determine the length of the interval is the average based. This average based uses an average-based method in determining the length of the interval [12].

Chen and Hsu in 2004 also developed a fuzzy time series. Chen and Hsu developed fuzzy time series by repartitioning based on frequency density. Chen and Hsu's frequency density repartitioning algorithm divides the interval with the highest frequency density into four sub-intervals, the interval with the second highest density into three sub-intervals, the interval with the third highest density into two sub-intervals, and the interval with the lowest density into one sub-interval.[6][13].

Based on the description above, the researcher is interested in modifying the frequency density partitioning algorithm used by Chen and Hsu, namely by exchanging the partition between the interval with the first densest frequency with the third densest interval, which was originally the first densest interval partitioned into 4 sub-intervals, the researcher changed the first densest was partitioned into 2 sub-intervals, and for the interval with the third densest frequency initially partitioned into 2 sub-intervals the researcher changed it to 4 sub-intervals.

Furthermore, the researcher will use the average-based method to determine the interval length in the fuzzy time series type Markov chain, and apply it to forecasting new positive cases of COVID-19 in Central Java.

#### METHODS

#### **Fuzzy Time Series**

The definition of fuzzy time series was first introduced by Song dan Chisom (1993). Let *U* universe of discourse, with  $U = \{u_1, u_2, ..., u_n\}$  on a fuzzy set  $A_i$ , defined as[3]:

$$A_{i} = \frac{f_{A}(u_{1})}{u_{1}} + \frac{f_{A}(u_{2})}{u_{2}} + \dots + \frac{f_{A}(u_{n})}{u_{n}}$$
(1)

where  $f_A$  is the membership of the fuzzy set  $A_i$  and  $u_k$  is an element of the fuzzy set  $A_i$  and  $f_A(u_k)$  shows the degree of membership of  $u_k$  in  $A_i$  where k = 1,2,3,...,n. **Definition.** If F(t) is caused by F(t - 1), then the relation in the first order model F(t) can be stated as follows: [5].

$${B \atop F(t)} = F(t-1) \circ R(t,t-1)$$
 (2)

where " $\circ$ " is Max-Min composition operator, and R(t, t - 1) is a relation matrix to describe the fuzzy relationship between F(t - 1) dan F(t).

#### Average-Based

Average based is an algorithm that can be used to set the interval length that is determined at the initial stage of forecasting when using fuzzy time series. The steps of the average based algorithm are as follows [12], [14]:

a. Determine the absolute difference (lag) between data n + 1 and data n with the formula:

$$lagD_n = |(Data \ n+1) - (Data \ n)| \tag{3}$$

b. Determine the length of the interval

$$length of interval = \left(\frac{total lag}{numbers of data}\right):2$$
(4)

c. Determine the basis value of the interval length according to Table 1. Following: Table 1. Basis Mapping Table

Range	Basis
0,1 - 1,0	0, <mark>1</mark>
1,1 -10	1
11-100	10
101-1000	100

d. The length of the interval is then rounded up according to the interval basis table.

#### **Modification Frequency Density Partition**

In this study, modifications to the frequency density partition were used, the algorithm used is as follows:

- a. The interval with the first densest frequency is divided into 2 subintervals.
- b. The interval with the second densest frequency is divided into 3 subintervals.
- c. The interval with the third densest frequency is divided into 4 subintervals
- d. Eliminates intervals that have no frequency.

#### Fuzzy Time Series Markov Chain

Markov Chain's Fuzzy Time Series forecasting procedure is as follows[10]: Step 1. Collecting historical data (*Yt*).

Step 2. Defines the U universe set of data, with D<sub>1</sub> and D<sub>2</sub> being the corresponding positive numbers.

$$U = [D_{min} - D1, D_{max} + D2]$$
(5)

Step 3. Specify the number of fuzzy intervals.

Step 4. Defining the fuzzy set in the universe of discourse U, the Fuzzy A<sub>i</sub> set declares the linguistic variable of the share price by  $1 \le i \le n$ .

Step 5. Fuzzification of historical data. If a time series data is included in the  $u_i$  interval, then that data is fuzzification into  $A_i$ .

Step 6. Specifies fuzzy logical relationship (FLR) and Fuzzy Logical Relationships Group (FLRG).

Step 7. Calculate forecasting results

For time series data, using FLRG, a probability can be obtained from a state heading to the next state. In order to calculate the predicting value, a Markov probability transition matrix with a dimension of  $n \times n$  was used. If

state  $A_i$  transition to a state  $A_j$  and pass the state  $A_k$ , i, j = 1, 2, ..., n, then we can obtain FLRG. The transition probability formula is as follows:

$$P_{ij} = \frac{M_{ij}}{M_i}, i, j = 1, 2, \dots, n$$
(6)

with:

 $P_{ij}$  = probability of transition from state  $A_i$  to state  $A_j$  one step  $M_{ij}$  = number of transitions from state  $A_i$  to state  $A_j$  one step

 $M_i$  = the amount of data included in the  $A_i$ 

The probability matrix R of all states can be written as follows:

$$R = \begin{bmatrix} P_{11} & \cdots & P_{1n} \\ \vdots & \ddots & \vdots \\ P_{n1} & \cdots & P_{nn} \end{bmatrix}$$
(7)

Matrix R reflects the transition of the entire system. If  $F(t-1) = A_i$ , then the process will be defined in the  $A_i$  at the time of (t-1), then the forecasting results F(t) will be calculated using the  $[P_{i1}, P_{i2}, ..., P_{in}]$  on the matrix R. Forecasting results F(t) is the weighted average value of the  $m_1$ ,  $m_2$ , ...,  $m_n$  (midpoint of  $u_1, u_2, ..., u_n$ ). The forecasting output result value on F(t) can be determined by using the following rules:

**Rule 1**: if fuzzy logical relationship group  $A_i$  is *one-to-one* (suppose  $A_i \rightarrow A_k$  where  $P_{ik} = 1$  and  $P_{ij} = 0, j \neq k$ ) then the forecasting value of F(t) is  $m_k$  the middle value of the  $u_k$ .

$$F(t) = m_k P_{ik} = m_k \tag{8}$$

**Rule 2:** if the FLRG  $A_i$  is one-to many (e.g.  $A_j \rightarrow A_1, A_2, ..., A_n$ . j = 1, 2, ..., n), when Y(t - 1) at time (t - 1) is included in state  $A_j$  then the forecasting F(t), is:

$$F(t) = m_1 P_{j1} + m_2 P_{j2} + \dots + m_{j-1} P_{j(j-1)} + Y(t - 1) P_{jj} + m_{j+1} P_{j(j+1)} + \dots + m_n P_{jn}$$
(9)

where  $m_1, m_2, ..., m_{j-1}, m_{j+1}, ..., m_n$  is the middle value  $u_1, u_2, ..., u_{j-1}, u_{j+1}, ..., u_n$ , and Y(t-1) are state values  $A_j$  at time t-1. **Rule 3:** if the FLRG  $A_i$  is empty  $(A_i \rightarrow \emptyset)$  forecast value F(t) is  $m_i$  which is the middle value of  $u_i$  with the following equation:

$$F(t) = m_i \tag{10}$$

Step 8. Adjusting the trend of forecasting values with the following rules:

• If state  $A_i$  communicates with  $A_i$ , starting from state  $A_i$  at time t - 1 expressed as  $F(t - 1) = A_i$ , and undergoing an increasing transition to state  $A_i$  at the time t where (i < j), then the adjustment value is:

$$D_{t1} = \left(\frac{l}{2}\right) \tag{11}$$

where *l* is the basis interval.

• If state  $A_i$  communicates with  $A_i$ , starting from state  $A_i$  at the time t - 1 expressed as  $F(t - 1) = A_i$ , and experiencing a decreasing transition to state  $A_j$  at the time t where (i > j) the adjustment value is:

$$D_{t1} = -\left(\frac{l}{2}\right)$$
(12)

• If state  $A_i$  at the time t - 1 is expressed  $F(t - 1) = A_i$ , and undergoes a jump forward transition to state  $A_{i+s}$  at the time t where  $(1 \le s \le n - i)$  then the adjustment value is:

$$D_{t2} = \left(\frac{l}{2}\right)s\tag{13}$$

where *s* is the number of forward jumps.

• If state  $A_i$  at the time t - 1 is as  $F(t - 1) = A_i$ , and undergoes a jumpbackward transition to *state*  $A_{i-v}$  at the time t where  $(1 \le v \le i)$  then the adjustment value is:

$$D_{t2} = -(\frac{l}{2})v$$
 (14)

where v is the number of jumps backward.

Step 9. Determine the final forecast value based on the adjustment of the trend of the forecasting value

If FLRG  $A_i$  is one-to-many and state  $A_{i+1}$  can be accessed from state  $A_i$  where state  $A_i$  is related to  $A_i$  then the forecasting result becomes  $'(t) = F(t) + D_{t1} + D_{t2} = F(t) + (\frac{l}{2}) + (\frac{l}{2})$ . If FLRG  $A_i$  is one-too-many and state  $A_{i+1}$  can be accessed from  $A_i$  where state  $A_i$  is not related to  $A_i$  then the forecasting values becomes  $F'(t) = F(t) + D_{t2} = F(t) + (\frac{l}{2})$ . If FLRG  $A_i$  is one to many and state  $A_{i-2}$  can be accessed from state  $A_i$  where  $A_i$  is not related to  $A_i$  then the forecasting result is  $F'(t) = F(t) - D_{t2} = F(t) - (\frac{l}{2}) \times 2 = F(t) - l$ . If v is jump step, the general form of the forecast is:

$$F'(t) = F(t) \pm D_{t1} \pm D_{t2} = F(t) \pm (\frac{l}{2}) \pm (\frac{l}{2}) v.$$
(15)

#### **Forecasting Error Measurement**

The reliability of a forecast can be determined by looking at mean average percentage error (MAPE), this MAPE formulas[15]:

$$MAPE = \frac{1}{n} \sum_{t=1}^{n} \frac{|Y(t) - F'(t)|}{Y(t)} x \ 100\%$$
(16)

with  $Y_t$ : actual data period t,  $F'_t$ : t period forecasting value, and n: the predictable amount of data.

#### **RESULTS AND DISCUSSION**

Forecasting with an average based-FTS Markov Chain with modified frequency density partitioning, the first step is to collect COVID-19 in the Central Java period June 25, 2021 until August 20, 2021 as a universe discourse (U). Next, determine the greatest value ( $D_{max} = 5655$ ) and smallest values ( $D_{min} = 1428$ ), and the value of D<sub>1</sub> = 8 and D<sub>2</sub> = 5, so it can be defined U = [1428 - 8, 5655 + 5] = [1420, 5660]. Then, calculate the absolute difference from historical data, the average absolute difference from 57 data points is 658,554, which is then divided by 2 to yield 329,277. The value of 329,277 is then determined using Table 1. The basis of the length of the interval is 100, so that U partitioned into can be the same interval length, namely  $u_1, u_2, u_3, u_4, u_5, \dots, u_{39}, u_{40}, u_{41}, u_{42}, u_{43}$  successively the value for each interval is

Table 2. Universe Discourse of New Positive Cases of Covid-19					
$u_1 = [1420, 1520]$	:				
$u_2 = [1520, 1620]$	$u_{41} = [5420, 5520]$				
$u_3 = [1620, 1720]$	$u_{42} = [5520, 5620]$				
$u_4 = [1720, 1820]$	$u_{43} = [5620, 5720]$				

The next step is to distribute the data to each interval and determine the frequency density, resulting in the densest interval, which is then repartitioned using a modified method. The following outcomes were achieved:

Interval		ensity and Repartition Interval Redivided interval
	Frequency	
$u_{29} = [4220, 4320]$	5	$u_{29,1} = [4220, 4270],$
		$u_{29,2} = [4270, 4320]$
$u_{28} = [4120, 4220]$	4	$u_{28,1} = [4120, 4153.33]$
		$u_{28,2} = [4153.33, 4186.67]$
		$u_{28,3} = [4186.67, 4220]$
$u_{16} = [2920, 3020]$	3	$u_{16,1} = [2920, 2945],$
		$u_{16,2} = [2945, 2970],$
		$u_{16,3} = [2970, 2995]$
		$u_{16,3} = [2995, 3020]$
$u_{17} = [3020, 3120]$	3	$u_{17,1} = [3020, 3045],$
		$u_{17,2} = [3045, 3070],$
		$u_{17,3} = [3070, 3095],$
		$u_{17,4} = [3095, 3120]$
$u_{19} = [3220, 3320]$	3	$u_{19,1} = [3220, 3245],$
		$u_{19,2} = [3245, 3270],$
		$u_{193} = [3270, 3295],$
		$u_{194} = [3295, 3320]$
$u_{27} = [4020, 4120]$	3	$u_{271} = [4020, 4045],$
		$u_{27,2} = [4045, 4070],$
		$u_{27,3} = [4070, 4095],$
		$u_{27,4} = [4095, 4120]$
$u_{32} = [4520, 4620]$	3	$u_{32,1} = [4520, 4545],$
52 1 9 9		$u_{32,2} = [4545, 4570],$
		$u_{32,3} = [4570, 4590],$
		$u_{32,4} = [4590, 4620]$
$u_{33} = [4620, 4720]$	3	$u_{33,1} = [4620, 4645],$
	5	$u_{33,2} = [4645, 4670],$
		$u_{33,2} = [1670, 1690],$ $u_{33,3} = [4670, 4695],$
		$u_{33,4} = [1695, 1695],$ $u_{33,4} = [4695, 4720]$
$u_2, u_3, u_4, u_5, u_6, u_8, u_{11}$	0	Removed
$u_{2}, u_{3}, u_{4}, u_{5}, u_{6}, u_{8}, u_{11}, u_{14}, u_{20}, u_{23}, u_{26}, u_{34}, u_{42}$	Ū	

Next, look for the middle value  $(m_1)$  for each interval, we get:

	Table 4. Middle Value					
$u_i$	$m_i$	$u_i$	$m_i$			
$u_1$	1470	:	:			
$u_7$	2070	$u_{39}$	5270			
$u_9$	2270	$u_{40}$	5370			
$u_{10}$	2370	$u_{41}$	5470			
$u_{12}$	2570	$u_{43}$	5670			

Furthermore, defining fuzzy sets, fuzzy sets that can be formed from the universe conversation are 44 fuzzy sets. The fuzzy sets formed is as follows:

$$A_{1} = \left\{ \frac{1}{u_{1}} + \frac{0.5}{u_{7}} + \frac{0}{u_{9}} + \frac{0}{u_{10}} + \dots + \frac{0}{u_{40}} + \frac{0}{u_{41}} + \frac{0}{u_{43}} \right\}$$

$$A_{2} = \left\{ \frac{0.5}{u_{1}} + \frac{1}{u_{7}} + \frac{0.5}{u_{9}} + \frac{0}{u_{10}} + \dots + \frac{0}{u_{40}} + \frac{0}{u_{41}} + \frac{0}{u_{43}} \right\}$$

$$A_{3} = \left\{ \frac{0}{u_{1}} + \frac{0.5}{u_{7}} + \frac{1}{u_{9}} + \frac{0.5}{u_{10}} + \dots + \frac{0}{u_{40}} + \frac{0}{u_{41}} + \frac{0}{u_{43}} \right\}$$

$$\vdots$$

$$A_{49} = \left\{ \frac{0}{u_{1}} + \frac{0}{u_{7}} + \frac{0}{u_{9}} + \frac{0}{u_{10}} + \dots + \frac{1}{u_{40}} + \frac{0.5}{u_{41}} + \frac{0}{u_{43}} \right\}$$

$$A_{50} = \left\{ \frac{0}{u_{1}} + \frac{0}{u_{7}} + \frac{0}{u_{9}} + \frac{0}{u_{10}} + \dots + \frac{0.5}{u_{40}} + \frac{1}{u_{41}} + \frac{0.5}{u_{43}} \right\}$$

$$A_{51} = \left\{ \frac{0}{u_{1}} + \frac{0}{u_{7}} + \frac{0}{u_{9}} + \frac{0}{u_{10}} + \dots + \frac{0}{u_{40}} + \frac{0.5}{u_{41}} + \frac{1}{u_{43}} \right\}$$

The next step is to perform fuzzification, the data from the fuzzification results are presented in the following table: Table 5 Euzzification Results

Table 5. Fuzzincation Results						
t	Actual Data	<i>fuzzy</i> Data	t	Actual Data	<i>fuzzy</i> Data	
1	2311	$A_3$	:	:	:	
2	2064	$A_2$	54	3263	$A_{18}$	
3	3079	$A_{14}$	55	3078	$A_{14}$	
4	2702	$A_6$	56	1428	$A_1$	
5	2932	$A_8$	57	1432	$A_1$	

The next step, determine the FLR and FLRG, as shown in Table 6. And Table 7:

Table 6. FLR

Data Order	FLR	Data Order	FLR
1-2	$A_3 \rightarrow A_2$	:	:
2-3	$A_2 \rightarrow A_{14}$	54-55	$A_{18} \rightarrow A_{14}$
3-4	$A_{14} \rightarrow A_6$	55-56	$A_{14} \rightarrow A_1$
4-5	$A_6 \rightarrow A_8$	56-57	$A_1 \to A_1$

Table 7. FLRG				
Current State	Next State	Current State	Next State	
A1	$(1)A_1$	:	:	
$A_2$	$(1)A_{14}$	$A_{49}$	$(1)A_{35}, (1)A_{42}$	
$A_3$	$(1)A_2$	$A_{50}$	$(1)A_{48}$	
$A_4$	$(1)A_{6}$	$A_{51}$	$(1)A_{43}$	

The initial forecast will be calculated next. For example, for t = 2, June 26, 2021, the forecast computation based on formulas (8), (9), and (10) is  $F(2) = m_k P_{ik} = m_k =$  2070. The summary of the initial forecasting results is as follows:

<b>Table 8.</b> Initial Forecasting Results $(F(t))$						
PeriodActual Data $F(t)$ PeriodActual Data $F(t)$						
6/25/21	2311	Na	÷	:	:	
6/26/21	2064	2070	8/19/21	1428	2070	
6/27/21	3078	3082,5	8/20/21	1432	1428	

After we get the initial forecasting, the next step is to adjust the forecasting trend. For example, adjustment value for June 26, 2021, the next step is  $A_2$  and the current state is  $A_3$  then the adjustment calculation uses the forecast adjustment rule (14) we get  $D_{t2} = -\left(\frac{l}{2}\right)v = -\left(\frac{100}{2}\right)1 = -(50)$ . Dor the calculation of other forecasting value adjustment using equations (11), (12), (13), and (14). The following is a forecast adjustment Table.

Table 8. Forecasting Trend Adjustment Value						
Period	FLR	$D_{tn}$	Period	FLR	$D_{t2}$	
6/25/21	$A_3 \rightarrow A_2$	Na		:	:	
6/26/21	$A_2 \rightarrow A_{14}$	-50	8/19/21	$A_{14} \rightarrow A_1$	-650	
6/27/21	$A_{14} \rightarrow A_9$	600	8/20/21	$A_1 \rightarrow A_1$	0	

Calculate the final forecast value. The final forecast is the sum of the initial forecast value with the forecast adjustment value by following the equation (15). For example, the final forecast value for June 26, 2021 data is  $F'_2 = F_2 \pm D_{t2} = 2070 + (-50) = 2020$ . By doing the same way, the summary of the final forecasting result is as follows:

Table. 9. Final Forecast Value					
Period	Y(t)	$F'_t$	Period	Y(t)	$F'_t$
6/25/21	2311	Na	:	:	1
6/26/21	2064	2020	8/19/21	1428	1907.5
6/27/21	3078	3682,5	8/20/21	1432	1428

Furthermore, the average based-FTS Markov chain is based on the modified frequency density partition to forecast data for new positive cases on August 21, 2021, the current state is  $A_1$ , from FLRG it is known that the next state of  $A_1$  is  $A_1$ , then based on equations (8), (9), and (10) the forecasting result is 1 times the data of the previous new positive case Y(t - 1) is 1432.

The last step is to calculate the forecast accuracy value using MAPE. The MAPE values of average based-FTS based on a modified frequency density partitioning is 10,7%. For forecasting results using average based-FTS based on a modified frequency density partitioning, are presented in the following figure:

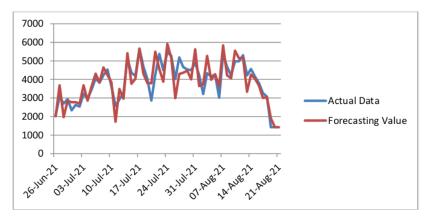


Figure 1. Graph of Forecasting Results Using Average Based-FTS Markov Chain Based on Modified Frequency Density Partitioning

#### CONCLUSIONS

Forecasting new positive cases of COVID-19 in Central Java using Average Based-FTS Markov Chain Based on Modified Frequency Density Partitioning has a good level of accuracy, this can be seen from the MAPE value obtained which is 10.7%. And for the predicted value of new positive cases on August 21, 2021, it is 1432 new positive cases of COVID-19 in Central Java.

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