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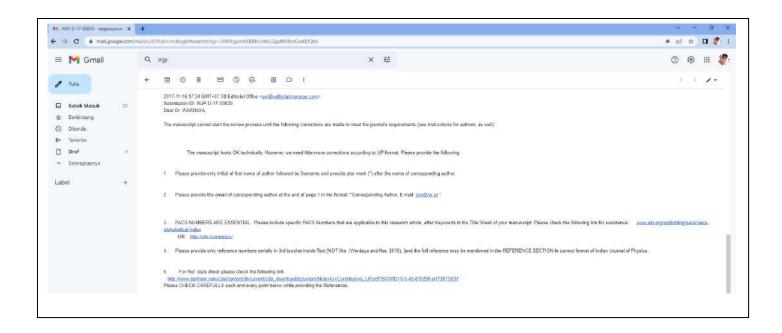
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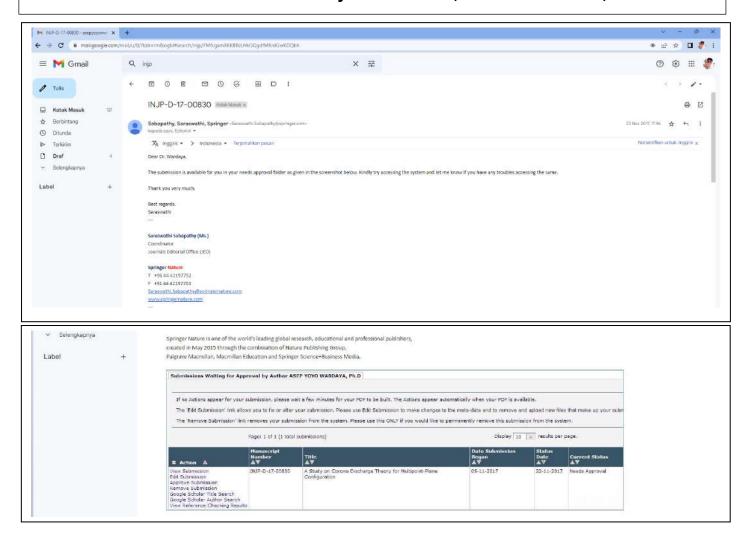




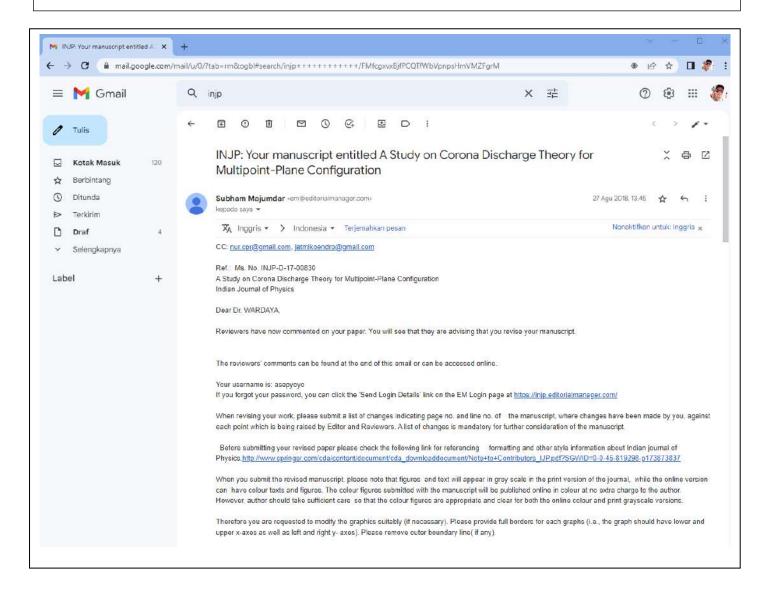
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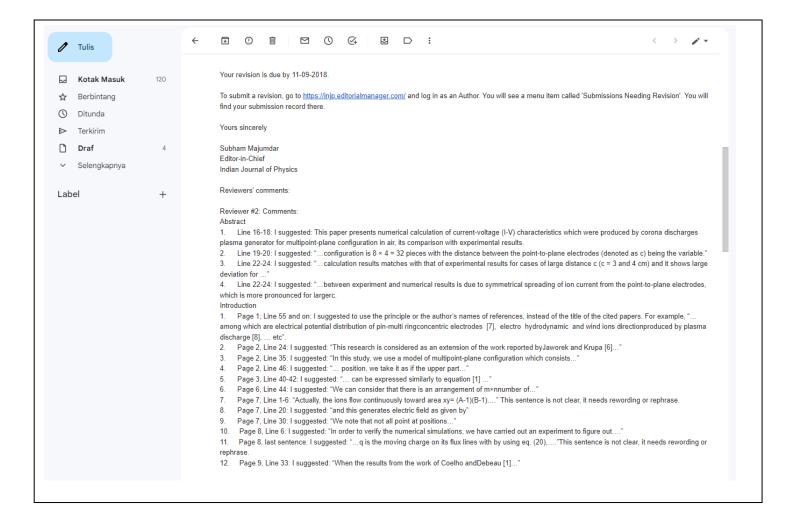


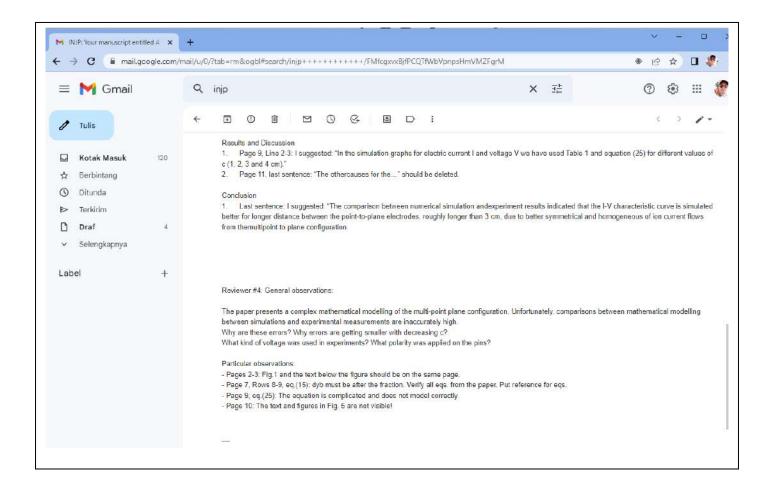
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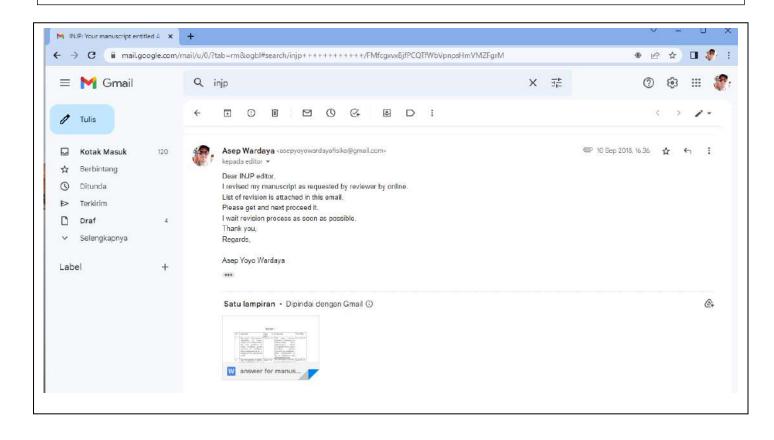
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Proses submission jurnal INJP, 10 September 2018



Answer for manuscript revision

Review 1

No	Sugestion	Line	or	Correction	New
		page			Page
1.	This paper with numerical calculations of current-voltage (I-V) characteristics that were produced by corona discharges plasma generator for multipoint-plane configuration in air, is compared with experimental results.	Line 18	16 -	This paper presents numerical calculation of current-voltage (I-V) characteristics which were produced by corona discharges plasma generator for multipoint-plane configuration in air, its comparison with experimental results.	Line 16 - 19
2.	The total number of needles in this configuration is $8 \times 4 = 32$ pieces and there is variation of c , which is the distance between the point-to-plane electrodes	Line 20	19-	The total number of needles in this configuration is $8 \times 4 = 32$ pieces with the distance between the point-to-plane electrodes (denoted as c) being the variable.	Line 19 - 23
3.	The $I-V$ characteristic curve of numerical calculation results matches that of experimental results for cases of large distance c (c = 3 and 4 cm) and does not match for cases of small distance c (c = 1 and 2 cm).	Line 24:	22-	The <i>I-V</i> characteristic curve of numerical calculation results matches with that of experimental results for cases of large distance c ($c = 3$ and 4 cm) and it shows large deviation for cases of small distance c ($c = 1$ and 2 cm).	26
4.	Differences in I-V	Line	25-	Differences in I-V characteristic curve	Line 26 -

		T		
	characteristic	27:	between experiment and numerical results	30
	curve between		is due to symmetrical spreading of ion	
	experiment and		current from the point-to-plane electrodes,	
	numerical results		which is more pronounced for larger c.	
	for cases of small c			
	is caused by more			
	symmetrical			
	spreading of ion			
	current from the			
	point-to-plane			
	electrodes for large			
	c cases than for			
	small c cases.			
	sman c cases.		Introduction	
1.	Some other	Page 1;		Page 1;
1.	research calculate	Line 55	related to corona discharges, among which	line 53 –
	values related to		_	
		and on	are electrical potential distribution of pin-	Page 2;
	corona discharges,		multi ring concentric	line 11.
	among which are		electrodes [7], electro hydrodynamic and	
	Electrical		wind ions direction produced by plasma	
	Potential		discharge [8], Ionic Wind Generation of	
	Distribution from		Needle-to-Cylinder Electrode Model [9],	
	EHD Flow Zone		Ionic Wind Generation of Multi Electrode	
	Using Pin-Multi		Model [10], Electro hydrodynamic Force	
	Ring Concentric		by A Corona Discharge [11].	
	Electrodes [7],		There are also research that discuss	
	Study of Electro		direct application of corona discharge	
	hydrodynamic and		electrode configuration, among those are	
	Wind Ions		Cold Large-Diameter Plasma Jet of A	
	Direction.		Triple Electrode Model [12], Electric	
	Produced by		Potential Distribution of Various Electrode	
	Positive Corona		models [13], and Laser-Induced Streamer	
	Plasma Discharge		Corona Discharge of A Needle-to-Plate	
	[8], Calculation of		Electrode Model [14].	
	Ionic Wind		. ,	
	Generation Using			
	Voltage and			
	Electric Current			
	Characteristics			
	from DC Needle-			
	to-Cylinder			
	Electrode Model			
	[9], Calculation of Ionic Wind			
	Generation Using			
	Geometrical			

Analysis of Multi		
Electrode Model		
Miniature Scaling		
(Gate Electrode		
and Collector		
Electrode) [10],		
Calculation of		
Electro		
hydrodynamic		
Force From Low		
Speed Electric		
Propulsion System		
Generated by A		
Corona Discharge		
between A Wire		
Active Electrode		
and Several		
Cylinder		
Electrodes [11].		
There are		
also research that		
discuss direct		
application of		
corona discharge		
electrode		
configuration,		
among those are		
Cold Large-		
Diameter Plasma		
Jet Near		
Atmospheric		
Pressure Produced		
by A Triple		
Electrode		
Discharge		
Configuration		
[12], Determining		
Electric Potential		
Distribution on		
Isolator Surfaces		
Exposed to Corona		
Discharges from		
Various Electrode		
Configurations		
[13], and		
Characteristics of		

	Laser-Induced Streamer Corona Discharge in A Needle-to-Plate Electrode System [14].			
2	This research is a continuation from the work of Jaworek and Krupa [6]	Page 2, Line 24	"This research is considered as an extension of the work reported by Jaworek and Krupa [6]"	Page 2; line 13 – 14.
3	This research uses a model of multipoint-plane configuration that consists	Page 2, Line 35:	"In this study, we use a model of multipoint-plane configuration which consists"	line 25.
4	position, take it as if the upper part	Page 3, Line 46:	" position, we take it as if the upper part"	Page 3; line 42.
5	can be stated as equation as [1]	Page 4, Line 40- 42:	" can be expressed similarly to equation [1]"	Page 4; line 40 - 42.
6	Say there is an arrangement of $m \times n$ number of	Page 6, Line 44:	"We can consider that there is an arrangement of m×n number of"	Page 6; line 40.
7.	",B-1, in discrete. Actually, the ions flow continuously toward area xy= (A-1)(B-1)" This sentence is not clear, it needs rewording or rephrase.	Page 7, Line 1-6:	B-1, where A and B are the number of maximum points on plate surface which exposed by ion current at coordinates of x and y respectively, in discrete numbers. These ion current will flow from needle tip to the plate surface with the maximum plate area is $xy = (A-1)(B-1)a^2$. Because ion current flux has the properties of symmetrical, homogeneous and continuous when arrive on plane configuration then discrete characteristic (summation form) in eq. (14) is become the continuous characteristic (integration form) of the electric field quantity that can be solved at eq (15) below.	Page 6; line 55 – Page 7; line 7.
8	and this generates electric field	Page 7, Line 20:	"and this generates electric field as given by"	Page 7; line 22.
9	Not all points at position	Page 7, Line 30:	"We note that not all point at positions"	Page 7; line 32.
10	An experiment to figure out	Page 8, Line 6:	"In order to verify the numerical simulations, we have carried out an	Page 8; line 5 –

			experiment to figure out"	7.
11	"q is the moving charge on its flux lines with by using eq. (20),"This sentence is not clear, it needs	Page 8, last sentence	"q is the charge of electric flux lines that is coming out of the multipoint to the plane configurations as defined in eq. (20),"	Page 9; line 1 – 2.
10	rewording or rephrase.	D 0	(433)	D 0
12	When Coelho dan Debeau [1]	Page 9, Line 33:	"When the results from the work of Coelho and Debeau [1]"	Page 9; line 38.
			sults and Discussion	
1	Using Table 1 and equation (25) for varied c of 1, 2, 3 and 4 cm results in simulation graphs for various electric current <i>I</i> and voltage <i>V</i> .	Page 10, Line 2-3:	"In the simulation graphs for electric current I and voltage V we have used Table 1 and equation (25) for different values of c (1, 2, 3 and 4 cm)."	Page 10; line 11 – 13.
2	The other causes for the slight mismatch between simulation and experiment results are errors in terms of measurement, electric device, and asymmetry	Page 11, last sentence:	deleted.	-
			Conclusion	
1	The comparison between modeling and experiment results stated more and more distance c then the I - V characteristic curve will nearest similar because more symmetrical and homogeneous of ion current flows from the multipoint to plane configuration.	Last sentence	The comparison between numerical simulation and experiment results indicated that the I-V characteristic curve is simulated better for longer distance between the point-to-plane electrodes, roughly longer than 3 cm, due to better symmetrical and homogeneous of ion current flows from the multipoint to plane configuration.	Last sentence

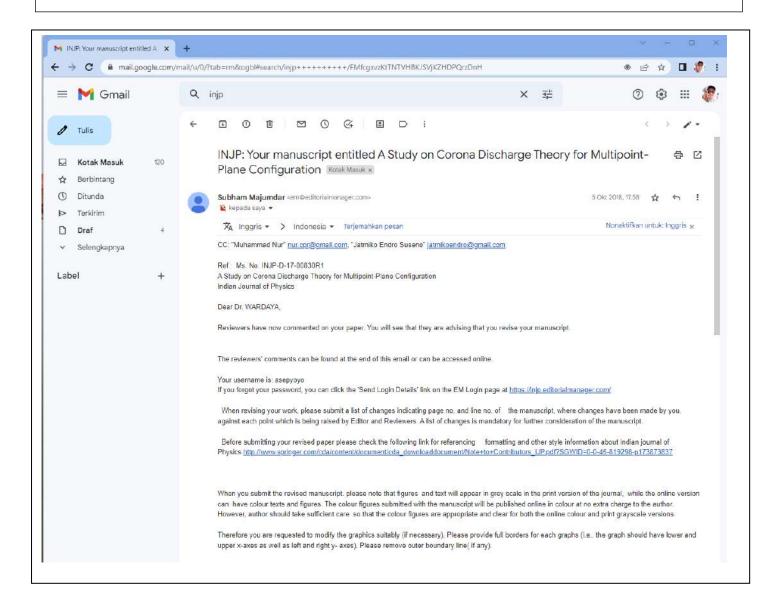
Review 2

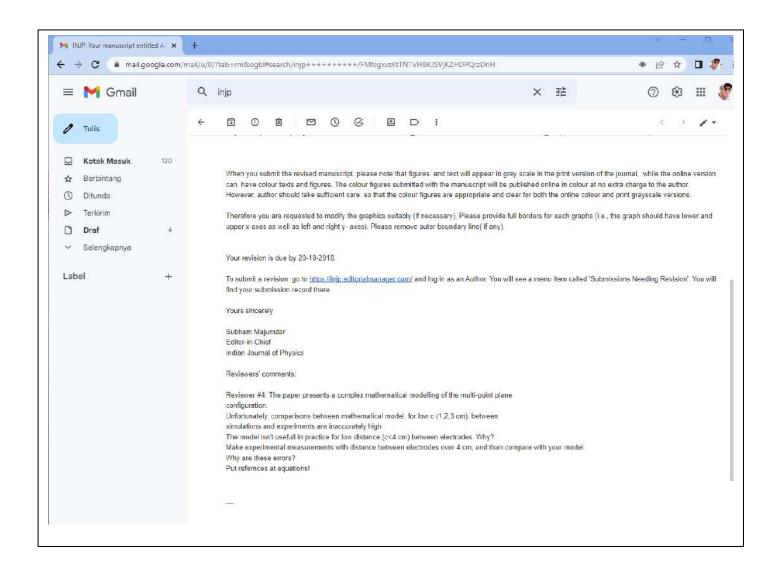
No	Sugestion	Line page	or	Correction	New Chapter,
1.	The paper presents a complex mathematical modelling of the multi-point plane configuration. Unfortunately, comparisons between mathematical modelling between simulations and experimental measurements are inaccurately high. Why are these errors? Why errors are getting smaller with decreasing c?			These statements can be explained as follows, Equation (14) shows the 3-dimensional vector of the ion current flow model which flows from needle tip to the bottom plate with the parabolic shape as shown in Figure 3. To simplify equation (14), we assume that the ion current flows symmetrically so that the flowing 3-dimensional vector will be changed become one direction of the upright axis (Z axis) because the ion current direction at the XY plane will be symmetrical circle therefore it will be eliminate each others. Another assumption is that the ion current in the direction of the Z axis will be homogenous distributed and close to continuous flowing, so that the vector and discrete (summation) characteristics in equation (14) changed be the continuous (integration) and scalar characteristics (only in the direction of the axis Z) in equation (15),	line and Page Results and Discussion, last sentence.
				where equation (15) is	

			part of equation (25). Therefore, the conditions of homogenous continuity and symmetry will be better for the distance of among the multipoint to the bottom plate surface is increaser, so that the mathematical simulation will be match the results of the experiment at the greater value of c.	
2.	What kind of voltage was used in experiments? What polarity was applied on the pins?	-	The Experiment of Corona discharge for multipoint- plane configuration uses DC voltage, with a positive polarity position at the point position and negative polarity at the plane position	_
3	Fig.1 and the text below the figure should be on the same page.	Pages 2-3.	Fig.1 and the text have been done on the same page.	Page 2, line 31 – 59.
4	eq.(15): dyb must be after the fraction. Verify all eqs. from the paper. Put reference for eqs.	Page 7, Rows 8 - 9.	A full explanation of the appearance of equation (15) is written in the results and discussion section. There are: "To simplify equation (14), we assume that the ion current flows symmetrically so that the flowing 3-dimensional vector will be changed become one direction of the upright axis (Z axis) because the ion current direction at the XY plane will be symmetrical circle therefore it will be eliminate each others. Another assumption is that the ion current in the	Discussion, Page 11,

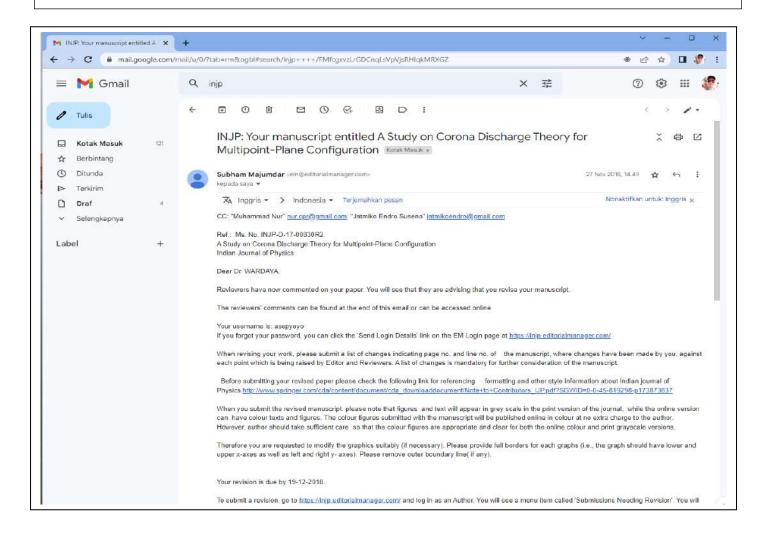
			direction of the Z axis will be homogenous distributed and close to continuous flowing, so that the vector and discrete (summation) characteristics in equation (14) changed be the continuous (integration) and scalar characteristics (only in the direction of the axis Z) in equation (15)". We have put references in equations of (1) - (7). The next equations do not have references because we calculate ourselves based on the condition of laboratory equipment and experimental models.	Page 3, line 17 – Page 5, line 7.
5	eq.(25): The equation is complicated and does not model correctly.	Page 9	Actually, model from the equation. (25) have described the real experiment result such as an ion flow calculation from multi-point to plane configurations which includes the calculation of the number of needles, parabolic trajectory of the electrical flux and the areas of the plane configuration that is exposed by electrical flux. So the equation can't be simplified and have explained in the chapter of results and discussion.	
6.	The text and figures in Fig. 5 are not visible!	Page 10.	The text and figures in Fig. 5 have been corrected.	Page 10.

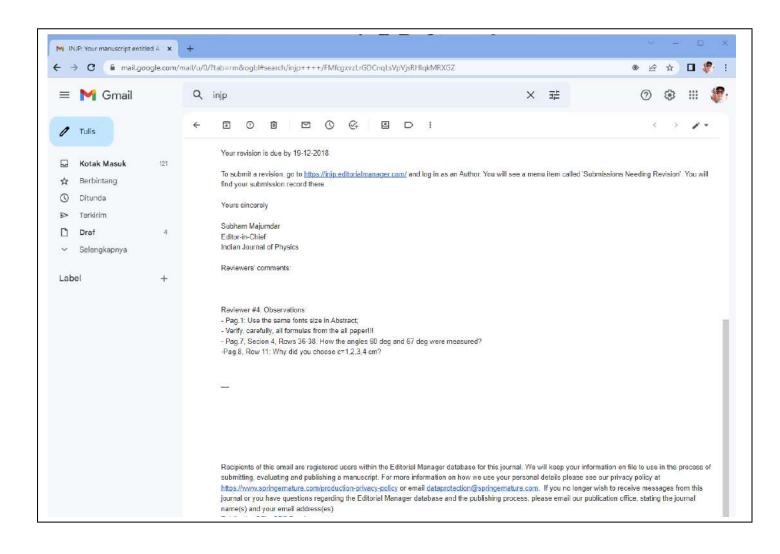
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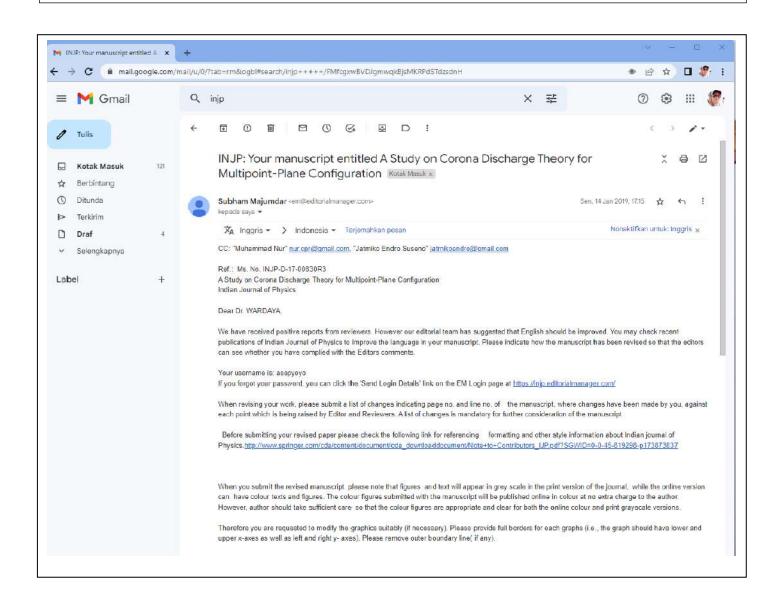


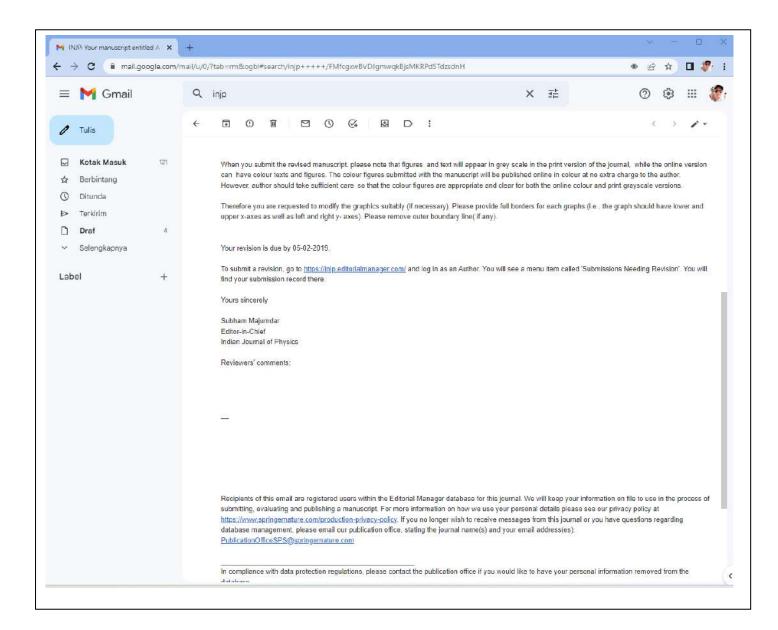
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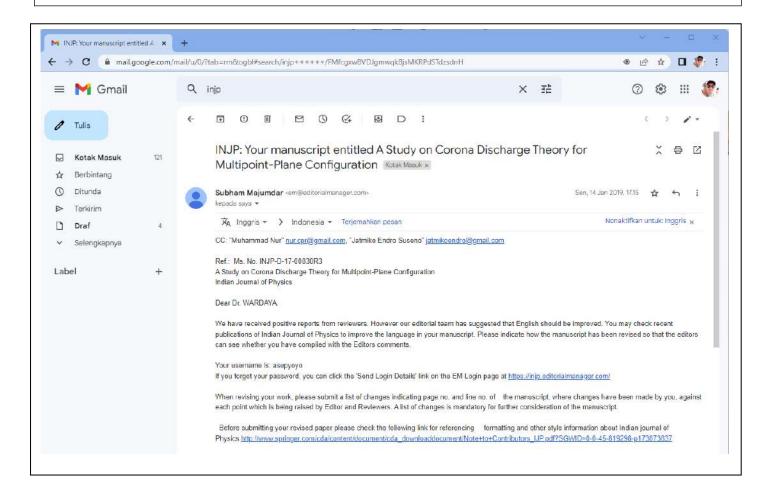


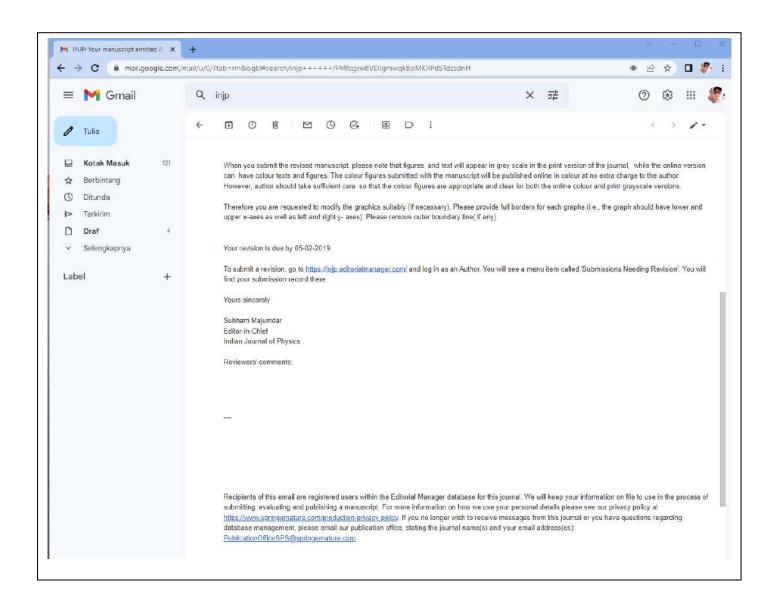
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Makalah Revisi

A Study of the Corona Discharge Theory for Multipoint-Plane Configurations

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Abstract: This paper presents the numerical calculation of current-voltage (I-V) characteristics that were

produced by a corona discharges plasma generator for a multipoint-plane configuration in air and; its

comparison with the experimental results. The total number of needles in this configuration is $8 \times 4 = 32$

with the distance between the point-to-plane electrodes (denoted as c) as the variable. The I-V

characteristic curve of the numerical calculation results matches that of the experimental results for cases

with a large distance c (c = 3 and 4 cm), and it shows a large deviation for cases with a small distance c (c

= 1 and 2 cm). Differences in the I-V characteristic curve between the experimental and numerical results

are due to the symmetrical spread of the ion current from the point-to-plane electrodes, which is more

pronounced for larger values of c.

Keywords: Plasma generator, multipoint-plane configuration, electric field, electric current, I-V

characteristics.

PACS Nos.: 02.30.-f; 02.30.Em; 02.30.Ik; 02.30.Mv; 02.70.-c

1. Introduction

The corona discharge technique has been widely used for various research studies. Some of the

papers on various electrode model configurations of corona discharges that try to obtain

potential, voltage, or electric current characteristic values include the tip-plane configuration [1],

thin bar-needle configuration [2], cylinder-wire-plate configuration [3], sub-millimeter electrode

gap configuration [4], point-to-ring configuration [5], and multipoint-plane configuration [6].

However, this paper discusses the current-voltage characteristics from the experimental results.

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Some other research studies have calculated values related to corona discharges, among which are electrical potential distribution of pin-multi-ring concentric electrodes [7], electrohydrodynamic and wind-ion direction produced

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by plasma discharge [8], ionic wind generation of needle-to-cylinder electrode model [9], ionic wind generation of multi electrode model [10], electro hydrodynamic force by a corona discharge [11].

There are also research studies that discuss the direct application of the corona discharge electrode configuration; cold large-diameter plasma jet of a triple electrode model [12], electric potential distribution of various electrode models [13], and laser-induced streamer corona discharge of a needle-to-plate electrode model [14].

This research is considered an extension of the work reported by Jaworek and Krupa [6] for the case of comparing the numerical calculation and experimental results of voltage and electric current characteristics generated by a corona discharge from plasma electrodes using a multipoint configuration. According to Sigmond [15], a large electric field generation along with a saturated current in the form of a corona discharge that, in turn, produces corona plasma is due to the sharp end of one of the electrodes; and the asymmetrical shape of both electrodes.

In this study, we use a model of a multipoint-plane configuration that consists of two perpendicular plates on one of which $m \times n$ number of needles is attached, as depicted in Fig. 1.

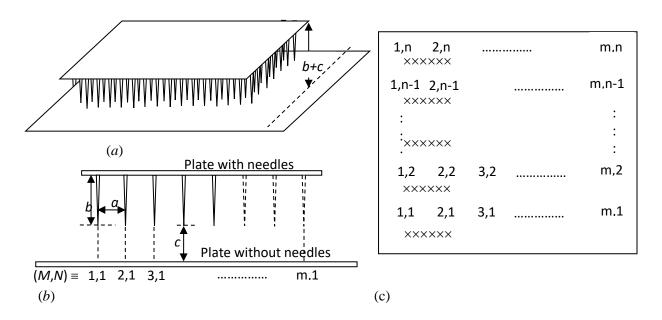


Figure 1. Model of the multipoint-plane configuration consisting of two parallel plates on one of which $m \times n$ needles are attached. The inter-needle distance is a, needle length is b, and distance between the point-to-plane electrodes is c. a). 3D representation of the electrode model. b). Side view of the electrode model. c). Top view of the location of $m \times n$ needles (marked \times).

As seen in Fig. 1, the needle length is b, inter-needle space is a, and distance between the point-to-plane electrodes is c. Hence, the distance between the two thin plates is b + c. The experiment of the corona discharge for the multipoint-plane configuration uses DC voltage; with a positive polarity position at the point position and negative polarity at the plane position.

2. Electric Field Intensity

The electric field generated by the corona discharge from the point-plane configuration can be calculated using a formula [1] that transforms hyperbolic coordinates into Cartesian coordinates as follows,

$$E(x, y, z) = \frac{\left[V/\ln\left(\frac{2}{\varepsilon}\right)\right]}{\sqrt{c^2 \cos^4 \xi + x^2 + y^2}},$$
(1)

where the hyperbolic coordinates (η, ξ, ψ) relate to the 3D Cartesian coordinates as follows [1]:

$$x = -c\cos\xi\sinh\eta\sin\psi; \quad y = -c\cos\xi\sinh\eta\cos\psi; \quad z = c\sin\xi\cosh\eta, \tag{2}$$

where [1]

$$\cos^2 \xi = \frac{u + \sqrt{u^2 + 4c^2(x^2 + y^2)}}{2c^2},\tag{3}$$

and [1]

$$u = c^{2} - (x^{2} + y^{2} + z^{2}) = c^{2} \cos^{2} \xi - \frac{(x^{2} + y^{2})}{\cos^{2} \xi},$$
 (4)

and V is the input voltage.

To calculate certain positions on the plate without the needle against the needle tip position, we perform the calculation as if the upper part of Fig. 1.a only has one needle at position (2, 2) in Fig. 1.c. The position without a needle is designated as (\bullet) , whereas the position with a needle is assigned as (\times) , as shown in Fig. 2.a, for a 2D representation in the xz coordinates. However,

seen from the z-axis, both position marks (\bullet) and (\times) for coordinate (2, 2) will coalesce as A_{00} . Therefore, a combination of those two marks in Fig. 2.b can simply be assigned as (\times).

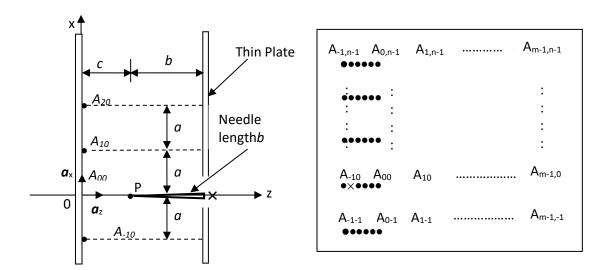


Figure 2. a);

Description of P points, A_{00} , A_{10} , A_{20} (marked \bullet) on the 2D xz-plane (y=0 and $z=\varsigma$, $\varsigma \Box 1$) that is induced by the electric current from the point-plane electrodes located in the positions marked (\times). b); Full description of the points on the xy-plane from the z point of view without taking P into account; A_{-10} , A_{00} , A_{10} , etc. Observed from z, the position of A_{00} (\bullet) coalesces with needle position (\times), so that mark \times is sufficient.

In Fig.2.a, a needle of length b (ending at point P), is attached on the plate (marked \times). The other points; $(A_{00}, A_{10}, A_{20}, ...)$ are at a distance of b+c from the plate with the needle, or points A_{00} , A_{10} , A_{20} , ...have a distance of $z = \varsigma$; $\varsigma \Box 1$ from the x-axis, where c is the distance from the needle tip to the plate without the needle.

The electric field generated by a needle electrode voltage source at point P with the coordinate $\xi = \frac{1}{2}\pi - \varepsilon$, where $\varepsilon \Box$ 1, and $\eta = 0$ (as x = y = 0, $z \sim c$, $u \sim 0$), can be expressed similarly to equation [1]:

$$E_{P} = E\left(\xi = \frac{1}{2}\pi - \varepsilon, \eta = 0\right) = \frac{\left[V/\ln\left(\frac{2}{\varepsilon}\right)\right]}{c\cos^{2}\left(\frac{1}{2}\pi - \varepsilon\right)},\tag{5}$$

where the relationship of the coordinate η and variables x and y is defined as follows [1]:

$$\eta = \tanh^{-1} \left\{ \frac{\sqrt{x^2 + y^2}}{z} \tan\left(\frac{1}{2}\pi - \varepsilon\right) \right\}. \tag{6}$$

Equation (6) indicates a high electric field at the needle tip (point P); due to the value of $\cos^2(\frac{1}{2}\pi - \varepsilon)\Box$ 1.

For the case at point A_{00} on the z-axis, with the distance c at the needle tip and its position at z = c; c = 1; c = 0, the resulting electric field at point c = 0 at position c = 0; is [1] as follows:

$$E_{00}\left(x=y=0,z\right) = \lim_{z\to 0} \frac{\left[\frac{cV}{\ln\left(\frac{2}{z}\right)}\right]}{\left(c^2-z^2\right)}.$$
 (7)

At another point $A_{\mu\nu}$ with $x = \mu a$ and $y = \nu a$; $\mu, \nu = 0, \pm 1, \pm 2,...$, the electric field induced by a point-plane electrode voltage source with the needle coalescing with the z-axis and its point at point P; is as follows:

$$E_{\mu\nu}\left(x = \mu a, y = \nu a, z = \varsigma\right) = \frac{\left[2cV/\ln\left(\frac{2}{\varepsilon}\right)\right]}{\sqrt{U_{\mu\nu}^{2} + 4(\mu^{2} + \nu^{2})c^{2}a^{2}}},$$
 (8)

where

$$U_{\mu\nu} = 2c^2 \cos^2 \xi = u_{\mu\nu} + \sqrt{u_{\mu\nu}^2 + 4c^2 a^2 (\mu^2 + \nu^2)} \quad , \tag{9}$$

and

$$u_{\mu\nu} = \lim_{z \to 0} \left[c^2 - \left(x^2 + y^2 + z^2 \right) \right] = \lim_{z \to 0} \left[c^2 - \left(\mu^2 + v^2 \right) a^2 - z^2 \right]. \tag{10}$$

The following commutative relationship with absolute value applies;

$$E_{\mu\nu} = E_{\nu\mu} = E_{|\mu|\nu|}; \ U_{\mu\nu} = U_{\nu\mu} = U_{|\mu|\nu|}; \ u_{\mu\nu} = u_{\nu\mu} = u_{|\mu|\nu|}. \tag{11}$$

3. Electric Field Superposition

When there are $m \times n$ needle electrodes inducing a homogeneous electric field at certain points (Fig. 1.c), then the electric field inducing those points can be calculated using the concept of the electric field vector superposition that stems from those needles. In general, the magnitude of the

electric field for points at $z = \zeta$, such as A_{00} , A_{20} , A_{14} , and so on. The calculation for the individual vector electric field where $x = \mu a$, y = va and $z = \zeta <<1$, is as follows:

$$\mathbf{E}_{\mu\nu}(x,y,z) = E_{\mu\nu}(\mu a, \nu a, \varsigma) \frac{\left\{x_{N} \mathbf{a}_{x} + y_{N} \mathbf{a}_{y} - c \mathbf{a}_{z}\right\}}{\sqrt{x_{N}^{2} + y_{N}^{2} + c^{2}}},$$
(12)

where x_N , y_N and $z_N = -c$, which is the length of a 3D vector from the needle tip to certain positions (M, N) (Fig. 1.b). The electric field on the plate without a needle (plane xy) will be calculated (point A_{00} is always at distance c from the needle tip). The total electric field at point (M, N) is a superposition of the individual electric fields that consists of $A \times B$ needle electrodes that induce the point (M, N), with $m \times n$ being the total number of needles; hence, $A \times B \le m \times n$; can be written as follows:

$$\left(\mathbf{E}_{T}\right)_{MN} = \sum_{\mu=0}^{A-1} \sum_{\nu=0}^{B-1} \mathbf{E}_{\mu\nu}(x, y, z), \qquad M = 1, 2, ..., m. \text{ and } N = 1, 2, ..., n.$$
 (13)

Some indexing rules apply:

- 1. The index (M, N) is a fixed position index on the *xy*-plane that relates to the number of needles $(m \times n)$.
- 2. The index μ , ν is the variable position index from point coordinate A_{ij} at position ($x = \mu a$, $y = \nu a$, $z = \zeta$) from the central coordinate (0, 0, 0) point of view, in which the reference point A_{00} is a position at distance c from the needle tipat the fixed index needle position (M, N).
- 3. The notations x_N , y_N and $z_N = -c$ are vector coordinates of the needle positions that stem from the needle tips and end at the points where the electric field is calculated on the plate without a needle (xy-plane).

The total electric field at certain positions (M, N) at distance c from the tip of the needles induced by the electric field generated by $A \times B$ needle electrodes (the total number of which is $m \times n$), based on equation (13) is as follows:

$$(\mathbf{E}_{T})_{\mathbf{MN}} = \sum_{\mu=0}^{A-1} \sum_{\nu=0}^{B-1} \left[E_{|M-1-\mu|,|N-1-\nu|} \right]_{\mu+1,\nu+1} \frac{\left\{ (M-1-\mu)a\mathbf{a}_{x} + (N-1-\nu)a\mathbf{a}_{y} - c\mathbf{a}_{z} \right\}}{\sqrt{\left((M-1-\mu)a \right)^{2} + \left((N-1-\nu)a \right)^{2} + c^{2}}},$$
 (14)

where M=1, 2, 3, ..., m and N=1, 2, 3, ..., n. This equation has electric field notation $E_{|M-1-\mu|,|N-1-\nu|}$ that which relates to equation (11).

We can consider that there is an arrangement of $m \times n$ needle electrodes as shown in Fig. 1.c. To calculate the electric field produced by each needle, at distance c from the needle tip, equation (14) is used. On the other hand, to calculate the total electric current produced by all needles, vector addition from each electric field unit in equation (14) must be performed. The total electric field resulting from all needles on the x- and y-axes will cancel each other out due to the symmetrical property, and what is left is the electric field components on the z-axis that will later be calculated.

Equation (14) describes the electric field resulting from the ions flow to the points at distances $x_{\alpha} = \alpha a$ and $y_{\beta} = \beta a$, with $\alpha = 0, 1, 2, ..., A-1$ and $\beta = 0, 1, 2, ..., B-1$, where A and B are the maximum points on the plate surface that exposed by the ion current at the x and y coordinates, respectively, in discrete numbers. These ion currents will flow from the needle tip to the plate surface with the maximum plate area of $xy = (A-1)(B-1)a^2$. Because the ion current flux has symmetrical, homogeneous, and continuous properties in the plane configuration, the discrete characteristics (summation form) in equation (14) become the continuous characteristics (integration form) of the electric field quantity that can be solved using equation (15);

$$(E_z)_{m \times n} = \frac{c}{a^2} \sum_{\alpha=0}^{A-1} \sum_{\beta=0}^{B-1} \int_{x=0}^{a\alpha} dx_{\alpha} \int_{y=0}^{a\beta} dy_{\beta} \frac{\left[VK_{|\alpha||\beta|} / \ln\left(\frac{2}{\varepsilon}\right) \right]}{\left(x_{\alpha}^2 + y_{\beta}^2 + c^2\right)}.$$
 (15)

Substitution from 2D Cartesian coordinates to the polar coordinates results in the following:

$$(E_{z})_{m \times n} = \frac{c}{a^{2}} \left[\frac{VK_{|\alpha||\beta|}}{\ln(\frac{2}{\varepsilon})} \right] \sum_{\alpha=0}^{A-1} \sum_{\beta=0}^{B-1} \int_{\rho=0}^{a\sqrt{\alpha^{2}+\beta^{2}}} \frac{\rho_{\alpha\beta}}{(\rho_{\alpha\beta}^{2}+c^{2})} d\rho_{\alpha\beta} \int_{\phi=0}^{2\pi} d\phi, \quad \rho_{\alpha\beta}^{2} = x_{\alpha}^{2} + y_{\beta}^{2}, \quad (16)$$

and this generates the electric field given by the following:

$$(E_z)_{m \times n} = \frac{\pi c}{a^2} \left[\frac{V}{\ln\left(\frac{2}{\varepsilon}\right)} \right] \sum_{\alpha=0}^{A-1} \sum_{\beta=0}^{B-1} K_{|\alpha||\beta|} \ln \left| \frac{a^2 \left(\alpha^2 + \beta^2\right) + c^2}{c^2} \right|. \tag{17}$$

4. Angle of Plasma Ion Flow

We note that not all points at positions $A_{\mu\nu}$; $\mu,\nu=0,\pm1,\pm2,...$, can be induced by the electric field. According to Nur et al. [8], the angular deviation of the plasma ion flow from the point location induced by the electric field to the perpendicular direction of the needle is around 60°, up to a maximum of 67°, as shown in Fig. 3.

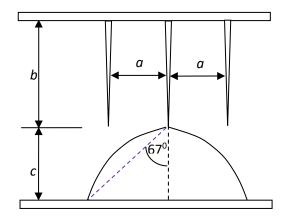


Figure 3. Maximum angular deviation of the electric field from the induced point location to the perpendicular direction of the needle is around 67° .

The relationship of θ and the position $A_{|\alpha||\beta|}$ can be calculated with the following equation:

$$\theta = \tan^{-1} \left\{ \frac{a}{c} \sqrt{\alpha^2 + \beta^2} \right\} \le 67^o, \text{ at position } A_{|\alpha||\beta|}.$$
 (18)

To verify the numerical simulations, we conducted an experiment to determine the relationship between the electric current I and voltage source V using a plasma discharge with multipoint-plane configuration, which has been performed at the Radiation Physics Laboratory at Diponegoro University. The needles were arranged in an $8 \times 4 = 32$ needle formation with a = 0.8068 cm, b = 0.018 cm and c was varied at 1 cm; 2 cm; 3 cm and 4 cm. The overall value of $K_{\alpha\beta}$ for the 8×4 needle configuration is as follows:

$$K_{00} = 32$$
; $K_{|0||\beta|} = K_{|\alpha||0|} = 64$ and $K_{|\alpha||\beta|} = 128$ for $\alpha, \beta = 1, 2, ..., 7$. (19)

The values of $A_{|\alpha||\beta|}$, index couple (α, β) ; and position number $K_{|\alpha||\beta|}$ for each variation of c, (taking equation (18) into account); are given in Table 1;

Table 1. Values of position $A_{|\alpha||\beta|}$, index couple (α, β) , and position number $K_{|\alpha||\beta|}$ for varied c.

No.	c	Position	(α, β)	$K_{ lpha eta }$
1.	1 cm	$egin{align} A_{00}, & A_{ 0 1 }, & A_{ 1 0 }, A_{ 1 1 }, \ & A_{ 1 2 }, A_{ 2 1 }, & A_{ 2 2 } \ \end{array}$	(0,0); (0,1); (1,0); (1,1); (1,2); (2,1); (2,2).	$K_{ 0 0 }$, $K_{ 0 1 }$, $K_{ 1 0 }$, $K_{ 1 1 }$, $K_{ 1 2 }$, $K_{ 2 1 }$, $K_{ 2 2 }$.
2.	2 cm	$A_{ 0 0 }$,, $A_{3 3 }$, $A_{ 3 4 }$	(0,0); $(0,1)$; $(1,0)$;;	$K_{ 0 0 }$,, $K_{ 3 3 }$, $K_{ 3 4 }$,

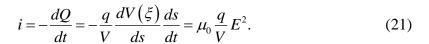
		$,A_{ 3 5 },A_{ 4 3 },A_{ 5 3 }.$	(3,3); (3, 4); (3,5); (4, 3)	$K_{ 3 5 }$, $K_{ 4 3 }$, $K_{ 5 3 }$.
			; (5, 3).	
3.	3 cm	A_{00} , $A_{ 0 1 }$, $A_{ 1 0 }$, $A_{ 1 1 }$,	(0,0); (0,1); (1,0);;	$K_{ 0 0 }$, $K_{ 0 1 }$, $K_{ 1 0 }$, ,
		$\dots, A_{ 6 6 }, A_{ 7 6 }, A_{ 6 7 }$	(6,6); (7,6); (6,7).	$K_{ 6 6 }$, $K_{ 7 6 }$, $K_{ 6 7 }$.
4.	4 cm	A_{00} , $A_{ 0\ 1 }$, $A_{ 1\ 0 }$, $A_{ 1\ 1 }$,	(0,0); (0,1); (1,0);;	
		$\dots, A_{ 7 6 }, A_{ 6 7 }, A_{ 7 7 }$	(6,6); (7,6); (6,7); (7,7).	$K_{ 6 6 }$, $K_{ 7 6 }$, $K_{ 6 7 }$, $K_{ 7 7 }$.

5. Induced Current

In the case of the point-plane configuration, the charge Q induced on the plane electrode becomes [1] the following;

$$Q = \frac{V(\xi) - V}{V} q,\tag{20}$$

where V is the potential of the point electrode and q is the charge of the electric flux lines coming from the multipoint to the plane configuration as defined in equation (20), and the induced current yields the following:



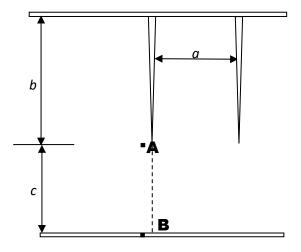


Figure 4. Electric field calculation on the plane electrode (B) positioned at distance c from the point electrode (A).

According to Halliday et al.[16], the electric field strength at point B can be written as follows:

$$E_{\mathcal{Q}} = \frac{q}{4\pi\varepsilon_0 c} \frac{1}{\left(b+c\right)} \ . \tag{22}$$

When the results from the work by Coelho and Debeau [1] are used as a comparison, the electric field strength at B located at distance c from the point electrode can be written as follows:

$$E_Q \cong \frac{V}{c \ln(\frac{2}{\epsilon})} . \tag{23}$$

Using equations (22) and (23), charge q is yielded as follows:

$$q = \frac{4\pi\varepsilon_0 (b+c)V}{\ln(\frac{2}{\varepsilon})} . \tag{24}$$

The electric current from the multipoint-plane configuration with 32 needles (N = 32) can be calculated using the equations (17), (21), and (24) as follows:

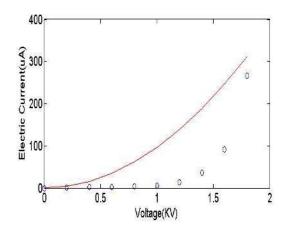
$$i = -N \frac{dQ}{dt}$$

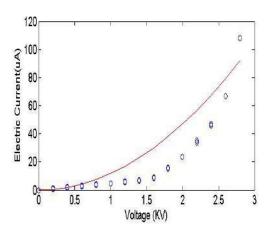
$$= \mu_0 N \frac{4\pi^3 \varepsilon_0 (b+c) c^2 V^2}{a^4 \ln^3 \left(\frac{2}{\epsilon}\right)} \left\{ \sum_{\alpha=0}^{A-1} \sum_{\beta=0}^{B-1} K_{|\alpha||\beta|} \ln \left| \frac{a^2 (\alpha^2 + \beta^2) + c^2}{c^2} \right| \right\}^2 \quad \text{with } \epsilon <<<1,$$
 (25)

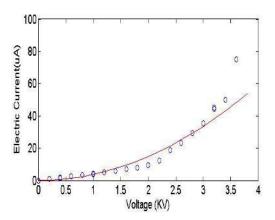
where μ_0 and ε_0 are the mobility $(4\pi \times 10^{-7} \text{Wb/A.m})$ and permittivity $(8,85 \times 10^{-12} \text{ F/m})$ at the vacuum space, respectively.

6. Results and Discussion

In the simulation graphs for the electric current I and voltage V, we use Table 1 and equation (25) for different values of c (1, 2, 3 and 4 cm). These simulation graphs are compared with experiment graphs of the same variations of electric current I and voltage V;







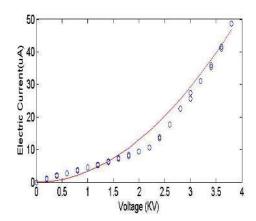


Figure 5. Graphs of the relationship between the electric current I and voltage source V obtained from the $8 \times 4 = 32$ needle electrode configuration, limited to 67° for the maximum deviation angle for a = 0.8068 cm, b = 0.018 cm, and varied c at 1; 2; 3 and 4 cm. Blue circles indicate the experiment results. Red lines show simulation results from equation (25).

A theory of corona discharge with multipoint-plane configuration has been discussed. The calculations of the electric field and saturated current generated from this configuration when input voltage V is applied have also been elaborated. The calculation of the total electric field resulting from $m \times n$ needle electrodes must be done using the concept of the electric field vector superposition. This research employs an arrangement of 8×4 needle electrodes with varied distances between the point-to-plane electrodes (c) at 1, 2, 3, and 4 cm.

The resulting graphs show that the simulation results are closer to the experiment results when the distance c is larger, especially for c at 3 cm and 4 cm. A narrower c causes an asymmetrical and inhomogeneous ion flow in which some areas are flooded with more ions than predicted. For a higher c, the symmetrical and homogeneous ion flow is closer to the experimental results. This causes an electric current reading that is closer to the expected value. Moreover, a narrower c does not allow the maximum electric field deviation angle from the induced point location to the perpendicular needle position, which may reach 67° , while greater c allows this to take place, hence, almost all ion flow that stems from the needle electrodes reaches all the designated points on the plane without the needles, and in turn, yields a greater

electric field. Another influencing factor for the electric current reading is the shape of the needle with a sharpness no closer than 0° , which is the ideal condition for electric field calculation.

These statements can be explained as follows, Equation (14) shows the 3D vector of the ion current flow model that flows from the needle tip to the bottom plate with a parabolic shape as shown in Fig. 3. To simplify equation (14), we assume that the ion current flows symmetrically so that the flowing 3D vector will be changed to one direction in the upright axis (z-axis) because the ion current direction at the xy-plane will be a symmetrical circle; therefore, it will eliminate the others. Another assumption is that the ion current in the direction of the z-axis will be homogenously distributed and close to continuously flowing, so that the vector and discrete (summation) characteristics in equation (14) are changed to continuous (integration) and scalar characteristics (only in the direction of the z-axis) in equation (15), where equation (15) is part of equation (25). Therefore, the conditions of homogenous continuity and symmetry will be better for an increased distance from the multipoint-plane to the bottom plate surface, so that the mathematical simulation will match the results of the experiment at a greater value of c.

7. Conclusion

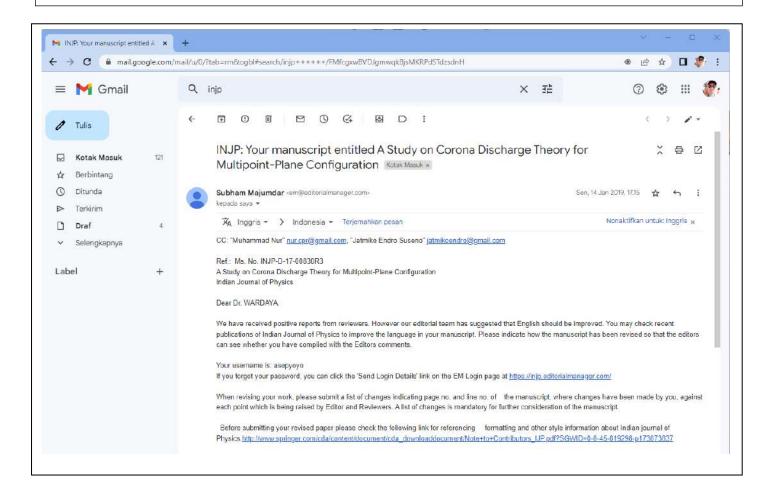
The current-voltage (I-V) characteristics that were produced by the corona discharge plasma generator for the multipoint-plane configuration in the air could demonstrate the performance of a device. The total electric field inducing these points could be calculated using the concept of the electric field vector superposition that stems from these needles. The total number of needles in this configuration is $8 \times 4 = 32$, and there is a variation of distance c, which is the distance between the point-to-plane electrodes. The between the numerical simulation and experimental results indicated that the I-V characteristic curve is simulated better for longer distances between the point-to-plane electrodes, which is roughly longer than 3 cm; due to better symmetry and homogeneity of the ion current flows from the multipoint-plane to the plane configuration.

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ORIGINAL PAPER





A study of the corona discharge theory for multipoint-plane configurations

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Abstract: This paper presents the numerical calculation of current–voltage (I-V) characteristics that were produced by a corona discharges plasma generator for a multipoint–plane configuration in air and its comparison with the experimental results. The total number of needles in this configuration is $8 \times 4 = 32$ with the distance between the point-to-plane electrodes (denoted as c) as the variable. The I-V characteristic curve of the numerical calculation results matches that of the experimental results for cases with a large distance c (c = 3 and 4 cm), and it shows a large deviation for cases with a small distance c (c = 1 and 2 cm). Differences in the I-V characteristic curve between the experimental and numerical results are due to the symmetrical spread of the ion current from the point-to-plane electrodes, which is more pronounced for larger values of c.

Keywords: Plasma generator; Multipoint-plane configuration; Electric field; Electric current; I-V characteristics

PACS Nos.: 02.30.-f; 02.30.Em; 02.30.Ik; 02.30.Mv; 02.70.-c

1. Introduction

The corona discharge technique has been widely used for various research studies. Some of the papers on various electrode model configurations of corona discharges that try to obtain potential, voltage, or electric current characteristic values include the tip-plane configuration [1], thin bar-needle configuration [2], cylinder-wire-plate configuration [3], sub-millimeter electrode gap configuration [4], point-to-ring configuration [5], and multipoint-plane configuration [6]. However, this paper discusses the currentvoltage characteristics from the experimental results. Some other research studies have calculated values related to corona discharges, among which are electrical potential distribution of pin-multi-ring concentric electrodes [7], electrohydrodynamic and wind-ion direction produced by plasma discharge [8], ionic wind generation of needle-tocylinder electrode model [9], ionic wind generation of multi-electrode model [10], electro hydrodynamic force by a corona discharge [11].

There are also research studies that discuss the direct application of the corona discharge electrode configuration; cold large-diameter plasma jet of a triple electrode model [12], electric potential distribution of various electrode models [13], and laser-induced streamer corona discharge of a needle-to-plate electrode model [14].

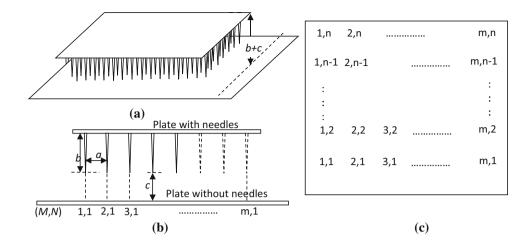
This research is considered an extension of the work reported by Jaworek and Krupa [6] for the case of comparing the numerical calculation and experimental results of voltage and electric current characteristics generated by a corona discharge from plasma electrodes using a multipoint configuration. According to Sigmond [15], a large electric field generation along with a saturated current in the form of a corona discharge that in turn produces corona plasma which is due to the sharp end of one of the electrodes and the asymmetrical shape of both electrodes.

In this study, we use a model of a multipoint-plane configuration that consists of two perpendicular plates on one of which $m \times n$ number of needles is attached, as shown in Fig. 1.

As seen in Fig. 1, the needle length is b, inter-needle space is a, and distance between the point-to-plane electrodes is c. Hence, the distance between the two thin plates

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Fig. 1 Model of the multipoint–plane configuration consisting of two parallel plates on one of which $m \times n$ needles are attached. The inter-needle distance is a, needle length is b, and distance between the point-to-plane electrodes is c. (a). 3D representation of the electrode model. (b). Side view of the electrode model. (c). Top view of the location of $m \times n$ needles (marked \times)



is b+c. The experiment of the corona discharge for the multipoint—plane configuration uses DC voltage; with a positive polarity position at the point position and negative polarity at the plane position.

2. Electric field intensity

The electric field generated by the corona discharge from the point–plane configuration can be calculated using a formula [1] that transforms hyperbolic coordinates into Cartesian coordinates as follows:

$$E(x, y, z) = \frac{\left[V/\ln(\frac{2}{\varepsilon})\right]}{\sqrt{c^2 \cos^4 \xi + x^2 + y^2}},\tag{1}$$

where the hyperbolic coordinates (η, ξ, ψ) relate to the 3D Cartesian coordinates as follows [1]:

$$x = -c\cos\xi\sinh\eta\sin\psi; \quad y = -c\cos\xi\sinh\eta\cos\psi; z = c\sin\xi\cosh\eta,$$

where [1]

$$\cos^2 \xi = \frac{u + \sqrt{u^2 + 4c^2(x^2 + y^2)}}{2c^2},\tag{3}$$

and [1]

$$u = c^{2} - (x^{2} + y^{2} + z^{2}) = c^{2} \cos^{2} \xi - \frac{(x^{2} + y^{2})}{\cos^{2} \xi},$$
 (4)

and V is the input voltage.

To calculate certain positions on the plate without the needle against the needle tip position, we perform the calculation as if the upper part of Fig. 1.a only has one needle at position (2, 2) in Fig. 1.c. The position without a needle is designated as "filled circle," whereas the position with a needle is assigned as \times , as shown in Fig. 2.a, for a 2D representation in the xz coordinates. However, seen

from the *z*-axis, both position marks "filled circle" and \times for coordinate (2, 2) will coalesce as A_{00} . Therefore, a combination of those two marks in Fig. 2.b can simply be assigned as (\times).

In Fig. 2.a, a needle of length b (ending at point P) is attached on the plate (marked \times). The other points (A_{00} , A_{10} , A_{20} , ...) are at a distance of b+c from the plate with the needle, or points A_{00} , A_{10} , A_{20} , ... have a distance of $z=\varsigma$; $\varsigma\ll 1$ from the x-axis, where c is the distance from the needle tip to the plate without the needle.

The electric field generated by a needle electrode voltage source at point P with the coordinate $\xi = \frac{1}{2}\pi - \varepsilon$, where $\varepsilon \ll 1$, and $\eta = 0$ (as x = y = 0, $z \sim c$, $u \sim 0$), can be expressed similarly to equation [1]:

$$E_P = E\left(\xi = \frac{1}{2}\pi - \varepsilon, \eta = 0\right) = \frac{\left[V/\ln(\frac{2}{\varepsilon})\right]}{c\cos^2(\frac{1}{2}\pi - \varepsilon)},\tag{5}$$

where the relationship of the coordinate η and variables x and y is defined as follows [1]:

$$\eta = \tanh^{-1} \left\{ \frac{\sqrt{x^2 + y^2}}{z} \tan\left(\frac{1}{2}\pi - \varepsilon\right) \right\}. \tag{6}$$

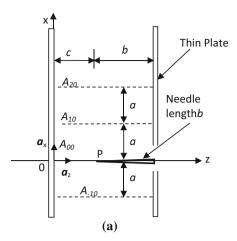
Equation (6) indicates a high electric field at the needle tip (point *P*) due to the value of $\cos^2(\frac{1}{2}\pi - \varepsilon) \ll 1$.

For the case at point A_{00} on the z-axis, with the distance c at the needle tip and its position at $z = \varsigma$; $\varsigma \ll 1$; $z \to 0$, the resulting electric field at point A_{00} at position x = y = 0 or $\eta = 0$ is [1] as follows:

$$E_{00}(x = y = 0, z) = \lim_{z \to 0} \frac{[cV/\ln(\frac{2}{z})]}{(c^2 - z^2)}.$$
 (7)

At another point $A_{\mu\nu}$ with $x = \mu a$ and $y = \nu a$, $\mu, \nu = 0, \pm 1$, $\pm 2,...$, the electric field induced by a point–plane electrode voltage source with the needle coalescing with the *z*-axis and its point at point *P* is as follows:

Fig. 2 (a) Description of P points, A_{00} , A_{10} , A_{20} (marked "filled circle") on the 2D xzplane (y = 0 and z = ς , $\varsigma \ll 1$) that is induced by the electric current from the point-plane electrodes located in the positions marked (\times) . (b) Full description of the points on the xy-plane from the z point of view without taking P into account, A_{-10} , A_{00} , A_{10} , etc. Observed from z, the position of A_{00} ("filled circle") coalesces with needle position (\times) , so that mark × is sufficient



A _{-1,n-1}	A _{0,n-1}	A _{1,n-1}		A _{m-1,n-1}		
:	:			:		
:	:			:		
	A ₀₀			A _{m-1,0}		
A ₋₁₋₁ A ₀₋₁ A ₁₋₁ A _{m-1,-1}						
(b)						

$$E_{\mu\nu}(x=\mu a, y=\nu a, z=\varsigma) = \frac{\left[2cV/\ln(\frac{2}{\varepsilon})\right]}{\sqrt{U_{\mu\nu}^2 + 4(\mu^2 + \nu^2)c^2a^2}},$$
(8)

where

$$U_{\mu\nu} = 2c^2 \cos^2 \xi = u_{\mu\nu} + \sqrt{u_{\mu\nu}^2 + 4c^2 a^2 (\mu^2 + \nu^2)}, \tag{9}$$

and

$$u_{\mu\nu} = \lim_{z \to 0} \left[c^2 - \left(x^2 + y^2 + z^2 \right) \right]$$

=
$$\lim_{z \to 0} \left[c^2 - \left(\mu^2 + v^2 \right) a^2 - z^2 \right].$$
 (10)

The following commutative relationship with absolute value applies

$$E_{\mu\nu} = E_{\nu\mu} = E_{|\mu||\nu|}; \quad U_{\mu\nu} = U_{\nu\mu} = U_{|\mu||\nu|}; u_{\mu\nu} = u_{\nu\mu} = u_{|\mu||\nu|}.$$
(11)

3. Electric field superposition

When there are $m \times n$ needle electrodes inducing a homogeneous electric field at certain points (Fig. 1c), the electric field inducing those points can be calculated using the concept of the electric field vector superposition that stems from those needles. In general, the magnitude of the electric field can be used for all points at $z = \zeta$, therefore the calculation for the individual vector electric field where $x = \mu a$, y = va and $z = \zeta \ll 1$, is as follows:

$$\mathbf{E}_{\mu\nu}(x, y, z) = E_{\mu\nu}(\mu a, \nu a, \varsigma) \frac{\{x_N \mathbf{a}_x + y_N \mathbf{a}_y - c \mathbf{a}_z\}}{\sqrt{x_N^2 + y_N^2 + c^2}}, \quad (12)$$

where x_N , y_N , and $z_N = -c$, which is the length of a 3D vector from the needle tip to certain positions (M, N) (Fig. 1.b). The electric field on the plate without a needle (plane xy) will be calculated. (Point A_{00} is always at distance c from the needle tip.) The total electric field at

point (M, N) is a superposition of the individual electric fields that consist of $A \times B$ needle electrodes that induce the point (M, N), with $m \times n$ being the total number of needles; hence, $A \times B \le m \times n$ can be written as follows:

$$(\mathbf{E}_{T})_{\mathbf{MN}} = \sum_{\mu=0}^{A-1} \sum_{\nu=0}^{B-1} \mathbf{E}_{\mu\nu}(x, y, z), \quad M = 1, 2, ..., m. \text{ and}$$

$$N = 1, 2, ..., n.$$
(13)

Some indexing rules apply:

- 1. The index (M, N) is a fixed position index on the xy-plane that relates to the number of needles $(m \times n)$.
- 2. The index μ , ν is the variable position index from point coordinate A_{ij} at position ($x = \mu a$, $y = \nu a$, $z = \zeta$) from the central coordinate (0, 0, 0) point of view, in which the reference point A_{00} is a position at distance c from the needle tip at the fixed index needle position (M, N).
- 3. The notations x_N , y_N , and $z_N = -c$ are vector coordinates of the needle positions that stem from the needle tips and end at the points where the electric field is calculated on the plate without a needle (xy-plane).

The total electric field at certain positions (M, N) at distance c from the tip of the needles induced by the electric field generated by $A \times B$ needle electrodes (the total number of which is $m \times n$) based on Eq. (13) is as follows:

$$(\mathbf{E}_{T})_{\mathbf{MN}} = \sum_{\mu=0}^{A-1} \sum_{\nu=0}^{B-1} \left[E_{|M-1-\mu|,|N-1-\nu|} \right]_{\mu+1,\nu+1} \frac{\left\{ (M-1-\mu)a\mathbf{a}_{x} + (N-1-\nu)a\mathbf{a}_{y} - c\mathbf{a}_{z} \right\}}{\sqrt{((M-1-\mu)a)^{2} + ((N-1-\nu)a)^{2} + c^{2}}},$$
(14)

where M=1, 2, 3,..., m and N=1, 2, 3,..., n. This equation has electric field notation $E_{|M-1-\mu|,|N-1-\nu|}$ which relates to Eq. (11).

We can consider that there is an arrangement of $m \times n$ needle electrodes as shown in Fig. 1.c. To calculate the electric field produced by each needle, at distance c from the needle tip, Eq. (14) is used. On the other hand, to calculate the total electric current produced by all needles, vector addition from each electric field unit in Eq. (14) must be performed. The total electric field resulting from all needles on the x- and y-axes will cancel each other out due to the symmetrical property, and what is left is the electric field components on the z-axis that will later be calculated.

Equation (14) describes the electric field resulting from the ions that flow to the points at distances $x_{\alpha} = \alpha a$ and $y_{\beta} = \beta a$, with $\alpha = 0, 1, 2, ..., A - 1$ and $\beta = 0, 1, 2, ..., B - 1$, where A and B are the maximum points on the plate surface that exposed by the ion current at the x and y coordinates, respectively, in discrete numbers. These ion currents will flow from the needle tip to the plate surface with the maximum plate area of $xy = (A - 1)(B - 1)a^2$. Because the ion current flux has symmetrical, homogeneous, and continuous properties in the plane configuration, the discrete characteristics (summation form) in Eq. (14) become the continuous characteristics (integration form) of the electric field quantity that can be solved using Eq. (15);

$$(E_z)_{m \times n} = \frac{c}{a^2} \sum_{\alpha=0}^{A-1} \sum_{\beta=0}^{B-1} \int_{x=0}^{a\alpha} dx_{\alpha} \int_{y=0}^{a\beta} dy_{\beta} \frac{\left[VK_{|\alpha||\beta|} / \ln(\frac{2}{\epsilon})\right]}{\left(x_{\alpha}^2 + y_{\beta}^2 + c^2\right)}$$
(15)

Substitution from 2D Cartesian coordinates to the polar coordinates results in the following:

$$(E_{z})_{m \times n} = \frac{c}{a^{2}} \left[\frac{VK_{|\alpha||\beta|}}{\ln(\frac{2}{\epsilon})} \right] \sum_{\alpha=0}^{A-1} \sum_{\beta=0}^{B-1} \int_{\rho=0}^{a\sqrt{\alpha^{2}+\beta^{2}}} \int_{\rho=0}^{\infty} \frac{\rho_{\alpha\beta}}{\left(\rho_{\alpha\beta}^{2}+c^{2}\right)} d\rho_{\alpha\beta} \int_{\phi=0}^{2\pi} d\phi, \quad \rho_{\alpha\beta}^{2} = x_{\alpha}^{2} + y_{\beta}^{2},$$
(16)

and this generates the electric field given by the following:

$$(E_{z})_{m \times n} = \frac{\pi c}{a^{2}} \left[\frac{V}{\ln(\frac{2}{\varepsilon})} \right] \sum_{\alpha=0}^{A-1} \sum_{\beta=0}^{B-1} K_{|\alpha||\beta|} \ln \left| \frac{a^{2} (\alpha^{2} + \beta^{2}) + c^{2}}{c^{2}} \right|.$$
(17)

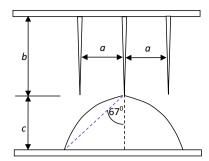


Fig. 3 Maximum angular deviation of the electric field from the induced point location to the perpendicular direction of the needle is around 67°

4. Angle of plasma ion flow

We note that not all points at positions $A_{\mu\nu}$, $\mu,\nu=0,\pm 1,\pm 2,...$ can be induced by the electric field. According to Nur et al. [8], the angular deviation of the plasma ion flow from the point location induced by the electric field to the perpendicular direction of the needle is around 60°, up to a maximum of 67°, as shown in Fig. 3.

The relationship of θ and the position $A_{|\alpha||\beta|}$ can be calculated with the following equation:

$$\theta = \tan^{-1} \left\{ \frac{a}{c} \sqrt{\alpha^2 + \beta^2} \right\} \le 67^\circ, \quad \text{at position } A_{|a||b|}. \quad (18)$$

To verify the numerical simulations, we conducted an experiment to determine the relationship between the electric current I and voltage source V using a plasma discharge with multipoint–plane configuration, which has been performed at the Radiation Physics Laboratory at Diponegoro University. The needles were arranged in an $8 \times 4 = 32$ needle formation with a = 0.8068 cm, b = 0.018 cm, and c was varied at 1 cm; 2 cm; 3 cm; and 4 cm. The overall value of $K_{\alpha\beta}$ for the 8×4 needle configuration is as follows:

$$K_{00}=32; K_{|0||\beta|}=K_{|\alpha||0|}=64$$
 and $K_{|\alpha||\beta|}=128$ for $\alpha,\beta=1,2,\ldots,7$. (19)

The values of $A_{|\alpha||\beta|}$ index couple (α, β) and position number $K_{|\alpha||\beta|}$ for each variation of c, [taking Eq. (18) into account] are given in Table 1.

5. Induced current

In the case of the point–plane configuration, the charge Q induced on the plane electrode becomes [1] the following:

Table 1	Values of po	Table 1 Values of position $A_{ \alpha \beta }$, index couple (α,β) , and position number $K_{ \alpha \beta }$ for varied c	$R_{ lpha eta }$ for varied c	
No.	C	Position	(α, β)	$K_{ m loulpi}$
1.	1 cm	$A_{00},A_{ 0 1 },A_{ 1 0 },A_{ 1 1 },A_{ 1 2 },A_{ 2 1 },A_{ 2 2 }$	(0,0);(0,1);(1,0);(1,1);(1,2);(2,1);(2,2)	$K_{ O O }, K_{ O I }, K_{ I O }, K_{ I I }, K_{ I I }, K_{ Z I }, K_{ Z I }$
2.	2 cm	$A_{[0 0 ,\dots,A_3 3 ,A_{[3 4 },A_{[3 5 },A_{[4 3 },A_{[5 3 }]}$	$(0,0);(0,1);(1,0);\ldots;(3,3);(3,4);(3,5);(4,3);(5,3)$	$K_{[0 0 ,\cdots,K_{ 3 3 },K_{ 3 4 },K_{ 3 5 },K_{ 4 3 },K_{ 5 3 }$
3.	3 cm	$A_{00}, A_{ 0 1 }, A_{ 1 0 }, A_{ 1 1 }, \ldots, A_{ 6 6 }, A_{ 7 6 }, A_{ 6 7 }$	$(0,0);(0,1);(1,0);\ldots;(6,6);(7,6);(6,7)$	$K_{[0 0 },K_{[0 1 },K_{ 1 0 },\ldots,K_{ 6 6 },K_{ 7 6 },K_{ 6 7 }$
4	4 cm	$A_{00},A_{ 0 1 },A_{ 1 0 },A_{ 1 1 },\ldots,A_{ 7 6 },A_{ 6 7 },A_{ 7 7 }$	$(0,0);(0,1);(1,0);\ldots;(6,6);(7,6);(6,7);(7,7)$	$K_{[0 0 },K_{[0 1 },K_{ 1 0 },\ldots,K_{ 6 6 },K_{ 7 6 },K_{ 6 7 },K_{ 7 7 }$

$$Q = \frac{V(\xi) - V}{V}q,\tag{20}$$

where V is the potential of the point electrode and q is the charge of the electric flux lines coming from the multipoint to the plane configuration as defined in Eq. (20), and the induced current yields the following (Fig. 4):

$$i = -\frac{dQ}{dt} = -\frac{q}{V}\frac{dV(\xi)}{ds}\frac{ds}{dt} = \mu_0 \frac{q}{V}E^2.$$
 (21)

According to Halliday et al. [16], the electric field strength at point B can be written as follows:

$$E_Q = \frac{q}{4\pi\varepsilon_0 c} \frac{1}{(b+c)}. (22)$$

When the results from the work by Coelho and Debeau [1] are used as a comparison, the electric field strength at B located at distance c from the point electrode can be written as follows:

$$E_Q \cong \frac{V}{c \ln(\frac{2}{\epsilon})}.$$
 (23)

Using Eqs. (22) and (23), charge q is yielded as follows:

$$q = \frac{4\pi\varepsilon_0(b+c)V}{\ln(\frac{2}{\varepsilon})}. (24)$$

The electric current from the multipoint–plane configuration with 32 needles (N = 32) can be calculated using Eqs. (17), (21), and (24) as follows:

$$i = -N \frac{dQ}{dt}$$

$$= \mu_0 N \frac{4\pi^3 \varepsilon_0 (b+c) c^2 V^2}{a^4 \ln^3 \left(\frac{2}{\varepsilon}\right)}$$

$$\left\{ \sum_{\alpha=0}^{A-1} \sum_{\beta=0}^{B-1} K_{|\alpha||\beta|} \ln \left| \frac{a^2 \left(\alpha^2 + \beta^2\right) + c^2}{c^2} \right| \right\}^2$$
with $\epsilon < < < 1$, (25)

where μ_0 and ϵ_0 are the mobility $(4\pi \times 10^{-7} \text{ Wb/A.m})$ and permittivity $(8.85 \times 10^{-12} \text{ F/m})$ at the vacuum space, respectively.

6. Results and discussion

In the simulation graphs for the electric current I and voltage V, we use Table 1 and Eq. (25) for different values of c (1, 2, 3, and 4 cm) (Fig. 5). These simulation graphs are compared with experiment graphs of the same variations of electric current I and voltage V;

A theory of corona discharge with multipoint-plane configuration has been discussed. The calculations of the

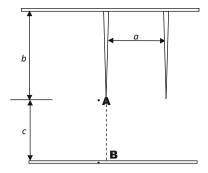


Fig. 4 Electric field calculation on the plane electrode (B) positioned at distance c from the point electrode (A)

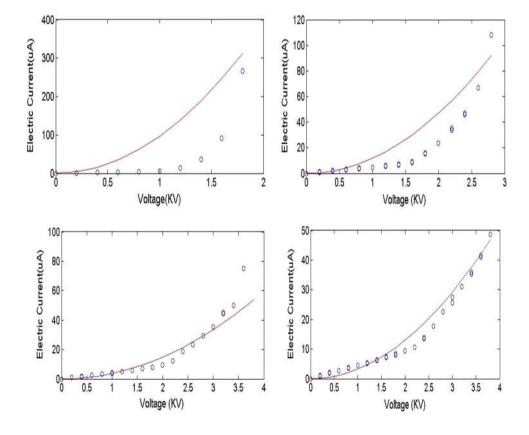
electric field and saturated current generated from this configuration when input voltage V is applied have also been elaborated. The calculation of the total electric field resulting from $m \times n$ needle electrodes must be done using the concept of the electric field vector superposition. This research employs an arrangement of 8×4 needle electrodes with varied distances between the point-to-plane electrodes (c) at 1, 2, 3, and 4 cm.

The resulting graphs show that the simulation results are closer to the experiment results when the distance c is larger, especially for c at 3 cm and 4 cm. A narrower c causes an asymmetrical and inhomogeneous ion flow in which some areas are flooded with more ions than predicted. For a higher c, the symmetrical and homogeneous

ion flow is closer to the experimental results. This causes an electric current reading that is closer to the expected value. Moreover, a narrower c does not allow the maximum electric field deviation angle from the induced point location to the perpendicular needle position, which may reach 67° , while greater c allows this to take place, hence, almost all ion flow that stems from the needle electrodes reaches all the designated points on the plane without the needles, and in turn, yields a greater electric field. Another influencing factor for the electric current reading is the shape of the needle with a sharpness no closer than 0° , which is the ideal condition for electric field calculation.

These statements can be explained as follows: Equation (14) shows the 3D vector of the ion current flow model that flows from the needle tip to the bottom plate with a parabolic shape as shown in Fig. 3. To simplify Eq. (14), we assume that the ion current flows symmetrically so that the flowing 3D vector will be changed to one direction in the upright axis (z-axis) because the ion current direction at the xy-plane will be a symmetrical circle; therefore, it will eliminate the others. Another assumption is that the ion current in the direction of the z-axis will be homogenously distributed and close to continuously flowing, so that the vector and discrete (summation) characteristics in Eq. (14) are changed to continuous (integration) and scalar characteristics (only in the direction of the z-axis) in Eq. (15), where Eq. (15) is part of Eq. (25). Therefore, the

Fig. 5 Graphs of the relationship between the electric current I and voltage source V obtained from the $8 \times 4 = 32$ needle electrode configuration, limited to 67° for the maximum deviation angle for a = 0.8068 cm, b = 0.018 cm, and varied c at 1, 2, 3, and 4 cm. Blue circles indicate the experiment results. Red lines show simulation results from Eq. (25)



conditions of homogenous continuity and symmetry will be better for an increased distance from the multipoint–plane to the bottom plate surface, so that the mathematical simulation will match the results of the experiment at a greater value of c.

7. Conclusion

The current-voltage (I-V) characteristics that were produced by the corona discharge plasma generator for the multipoint-plane configuration in the air could demonstrate the performance of a device. The total electric field inducing these points could be calculated using the concept of the electric field vector superposition that stems from these needles. The total number of needles in this configuration is $8 \times 4 = 32$, and there is a variation of distance c, which is the distance between the point-to-plane electrodes. The comparison between the numerical simulation and experimental results indicated that the I-V characteristic curve is simulated better for longer distances between the point-to-plane electrodes, which is roughly longer than 3 cm; due to better symmetry and homogeneity of the ion current flows from the multipoint-plane to the plane configuration.

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